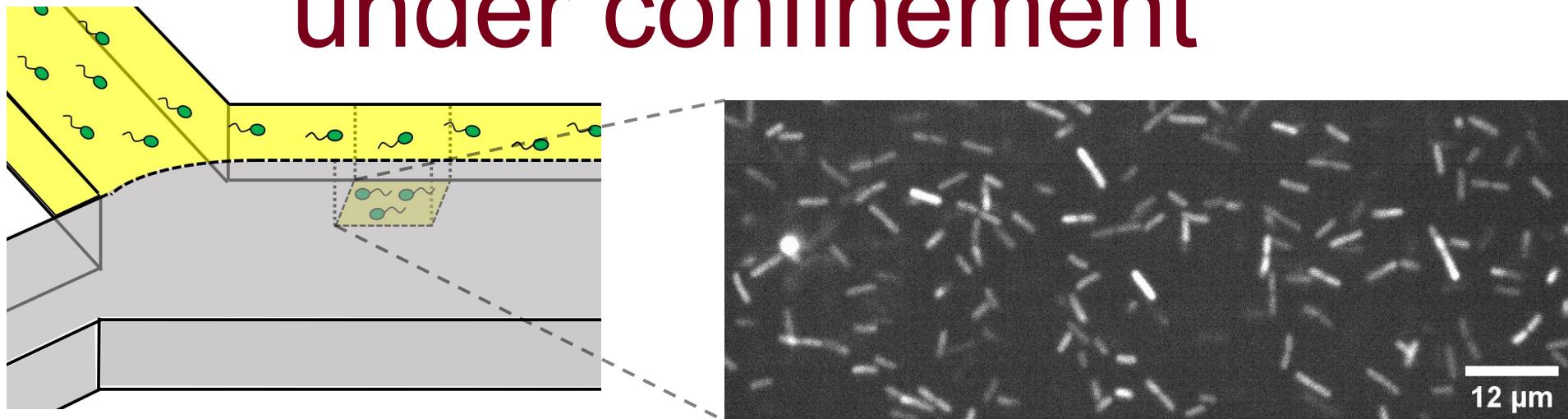


# Rheology of bacterial suspensions under confinement



Zhengyang Liu

Advisor: Xiang Cheng

91<sup>st</sup> Society of Rheology Meeting, Raleigh, 2019

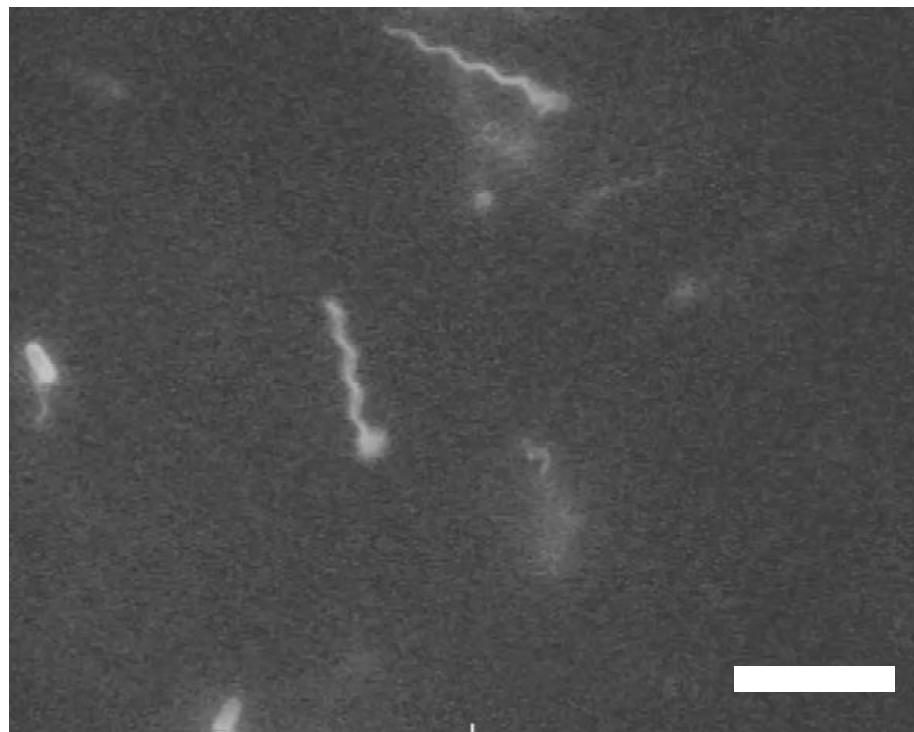
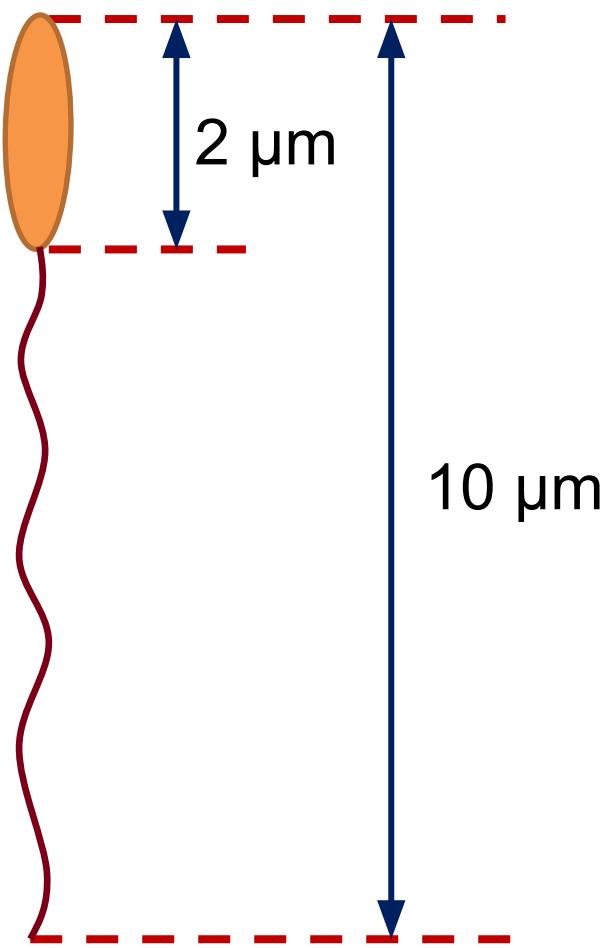
**M**  
UNIVERSITY OF MINNESOTA

**CEMS**

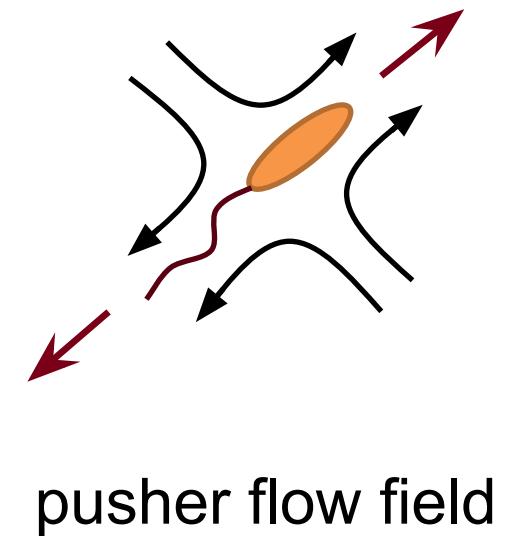
Chemical Engineering  
& Materials Science



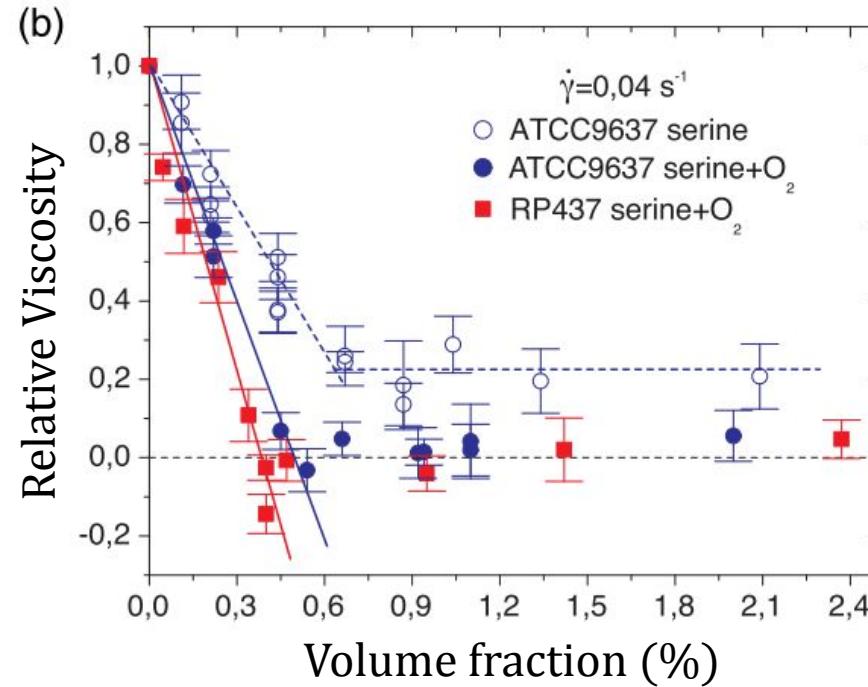
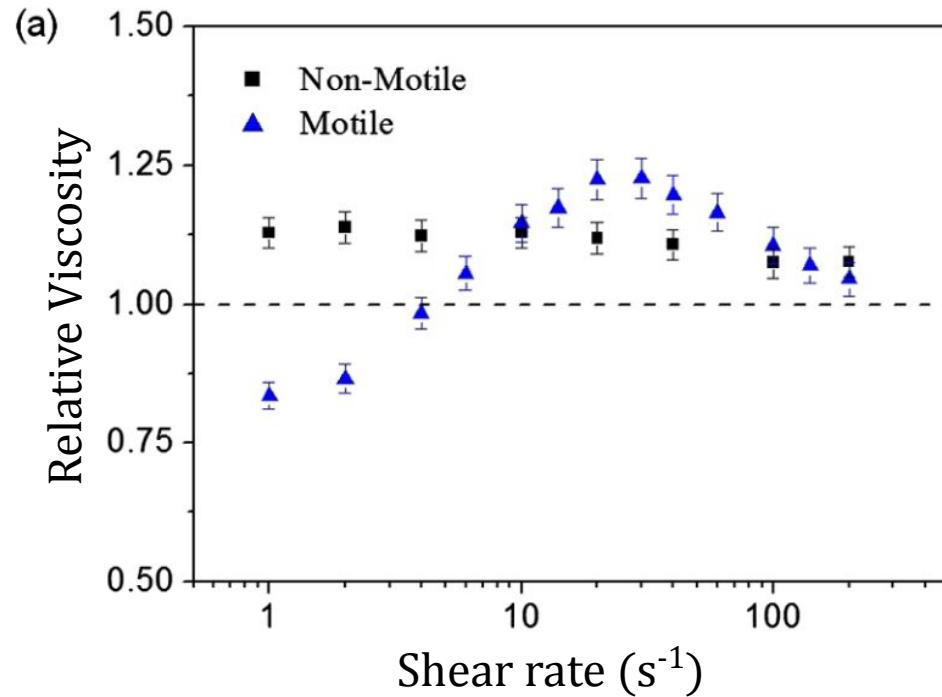
# *E. coli* – a model pusher swimmer



Turner et al., *J. Bacteriol.*, 2000 (Scale bar = 10  $\mu\text{m}$ )



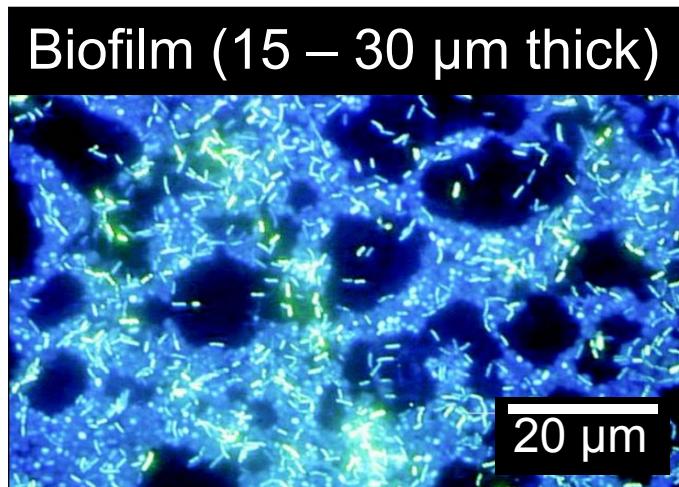
# Pushers reduce viscosity of bulk suspensions



- In contrast to passive particle suspensions, bacteria can **reduce** the viscosity of their suspending fluids
- Zero apparent viscosity “bacterial superfluid” can be achieved

# Bacterial suspensions under confinement

Natural processes



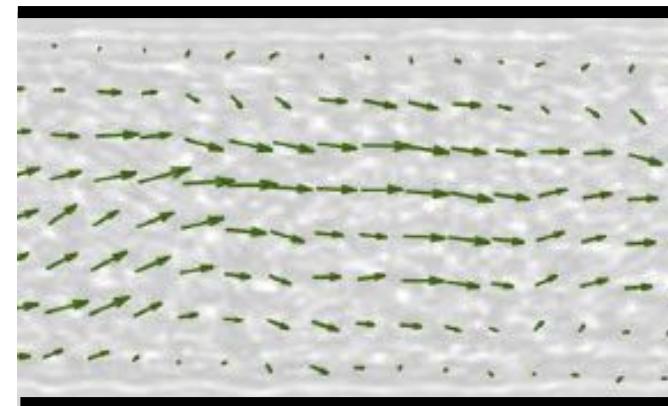
Donlan, *Emerg. Infect. Dis.*, 2002



Fundamental interest



Lushi et al., *PNAS*, 2014



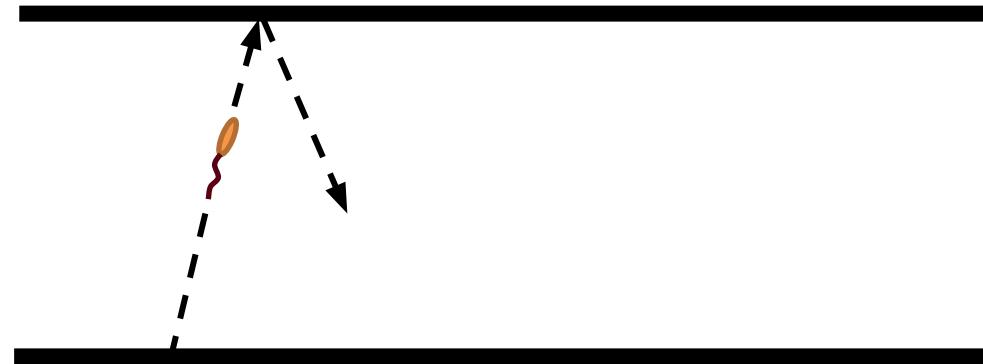
Wioland et al., *New J. Phys.*, 2016

# Bacterial dynamics under confinement

- Competing length scales

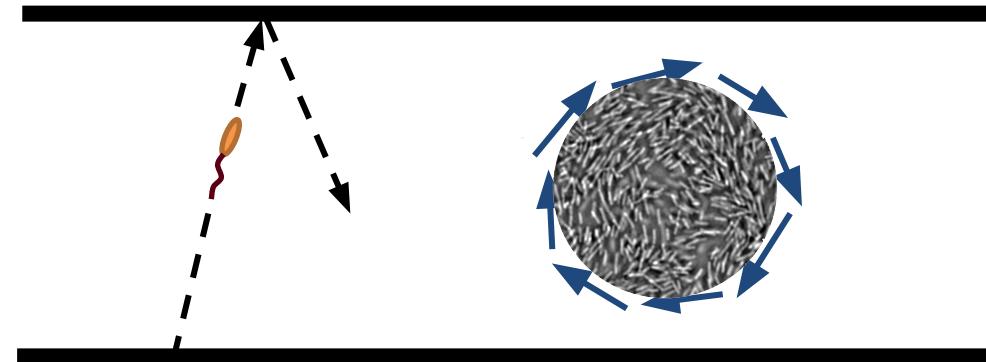
# Bacterial dynamics under confinement

- Competing length scales
  - **run length**



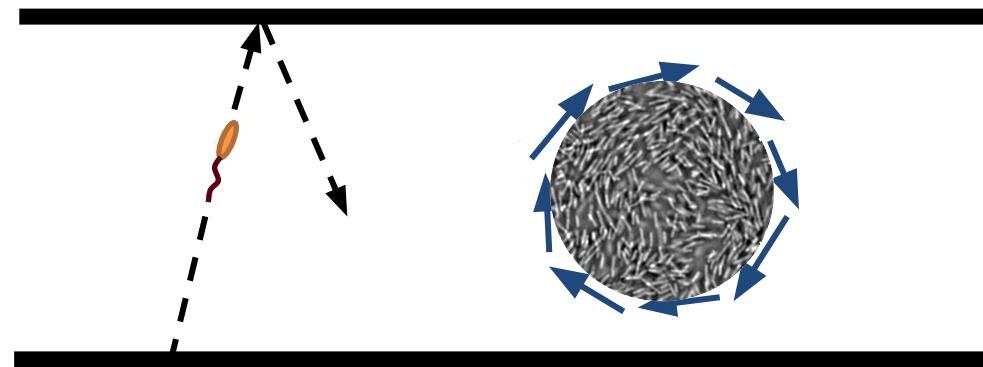
# Bacterial dynamics under confinement

- Competing length scales
  - run length
  - **vortex size**



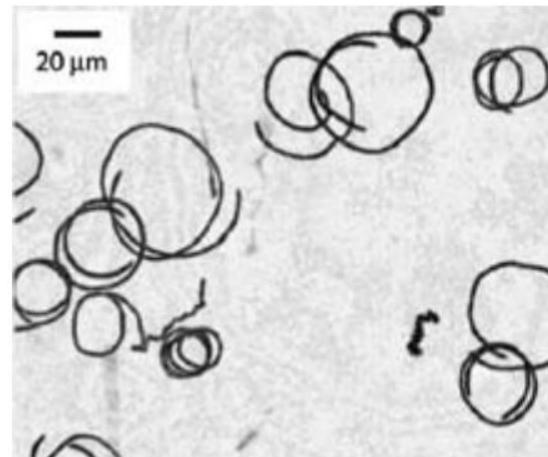
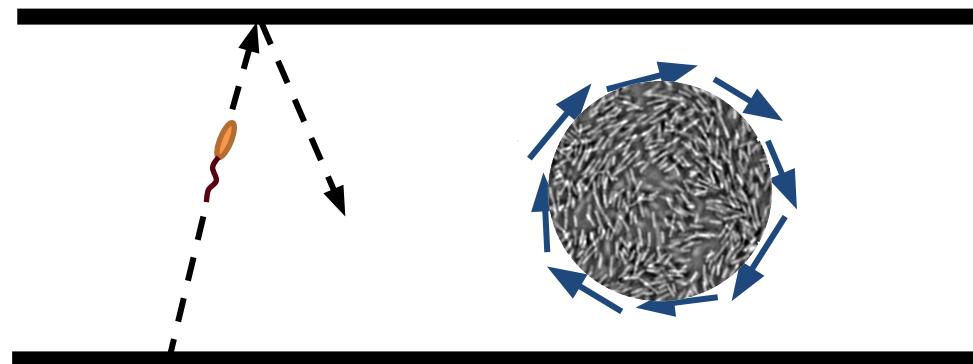
# Bacterial dynamics under confinement

- Competing length scales
  - run length
  - vortex size
- Swimmer-boundary Interaction



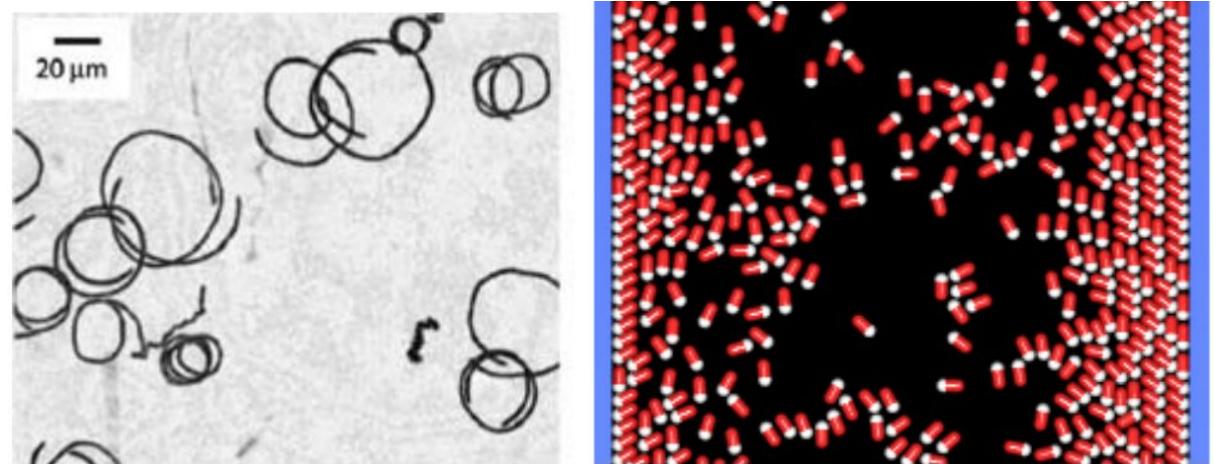
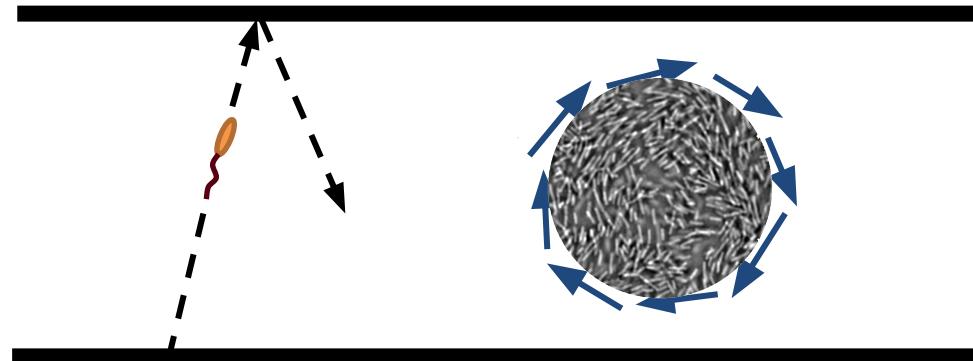
# Bacterial dynamics under confinement

- Competing length scales
  - run length
  - vortex size
- Swimmer-boundary Interaction
  - **hydrodynamic trapping**



# Bacterial dynamics under confinement

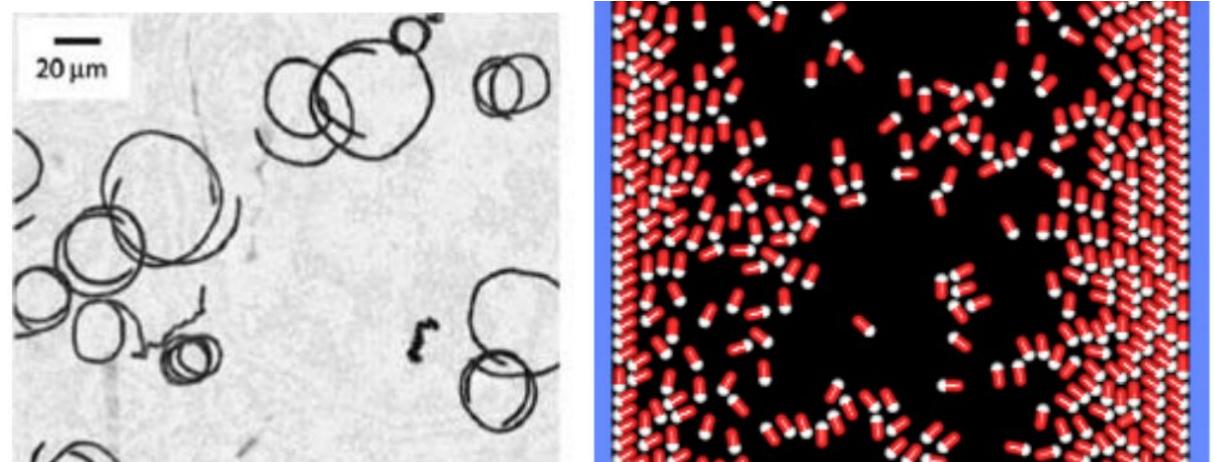
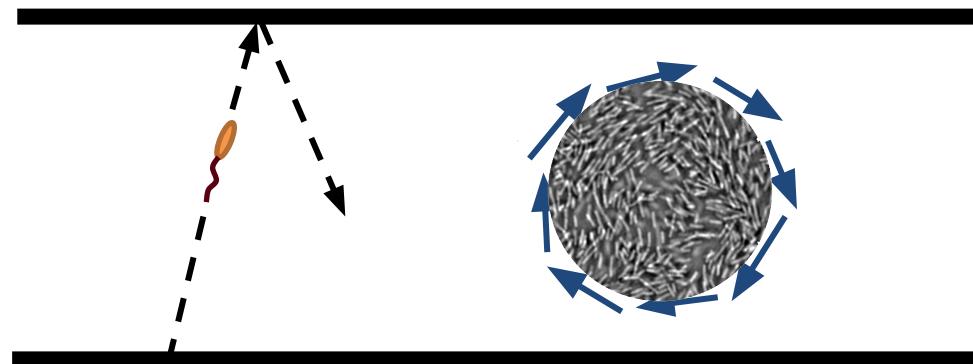
- Competing length scales
  - run length
  - vortex size
- Swimmer-boundary Interaction
  - hydrodynamic trapping
  - **upstream swimming**



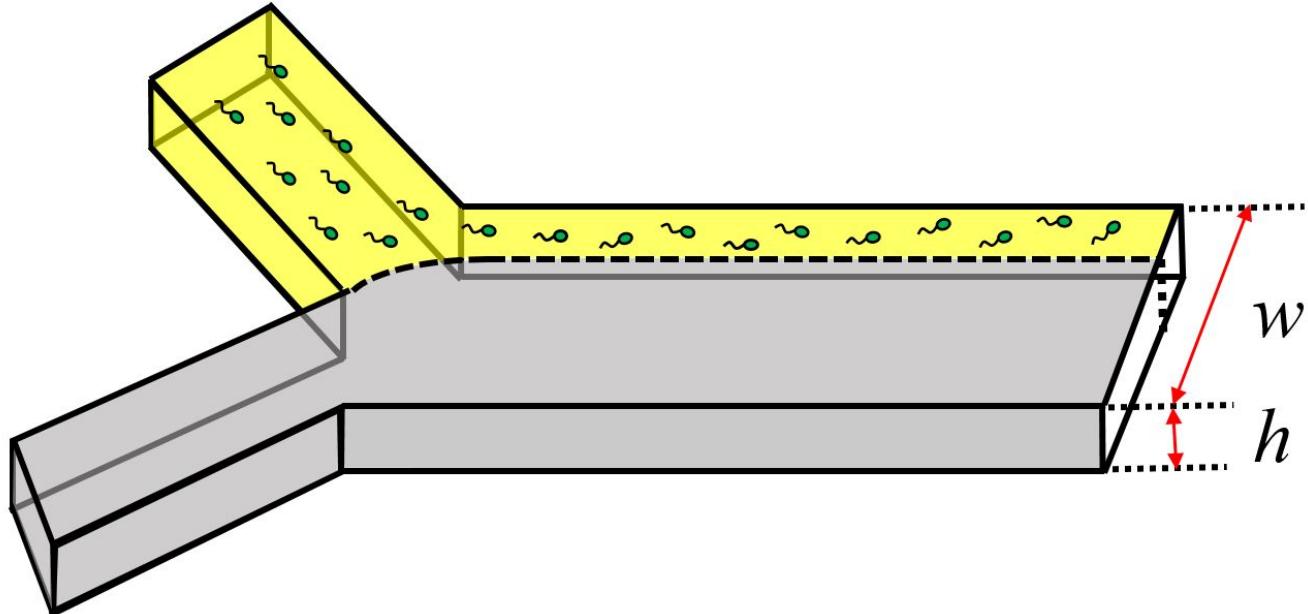
# Bacterial dynamics under confinement

- Competing length scales
  - run length
  - vortex size
- Swimmer-boundary Interaction
  - hydrodynamic trapping
  - upstream swimming

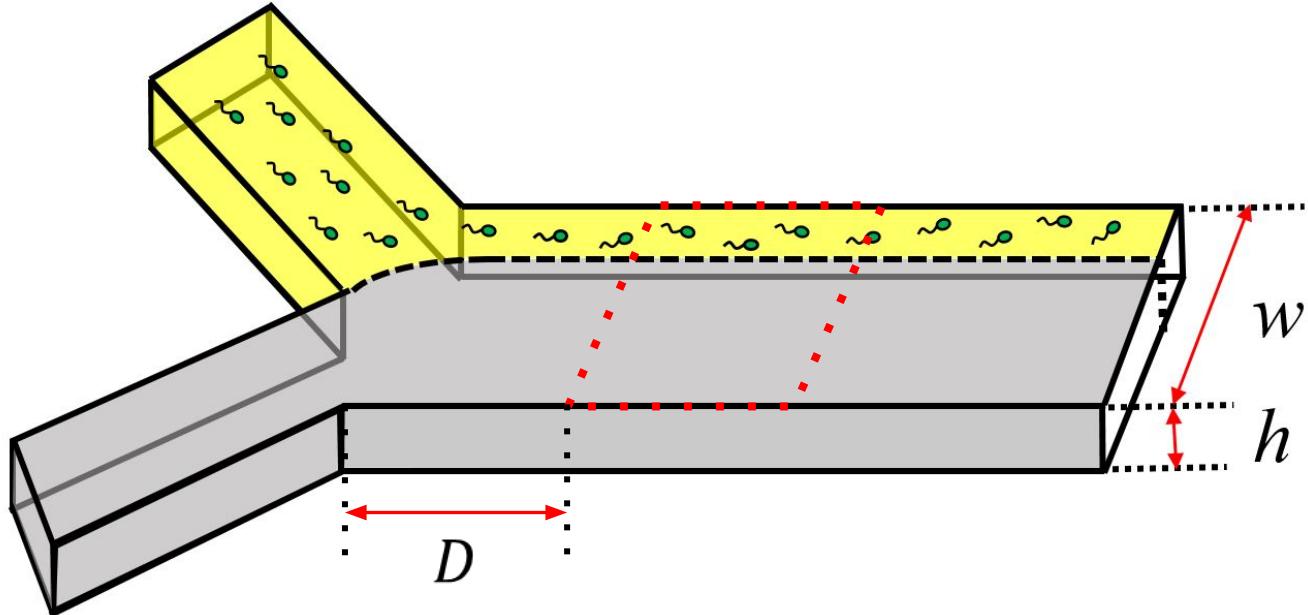
Different rheology under confinement?



# Microfluidic channel viscometer



# Microfluidic channel viscometer



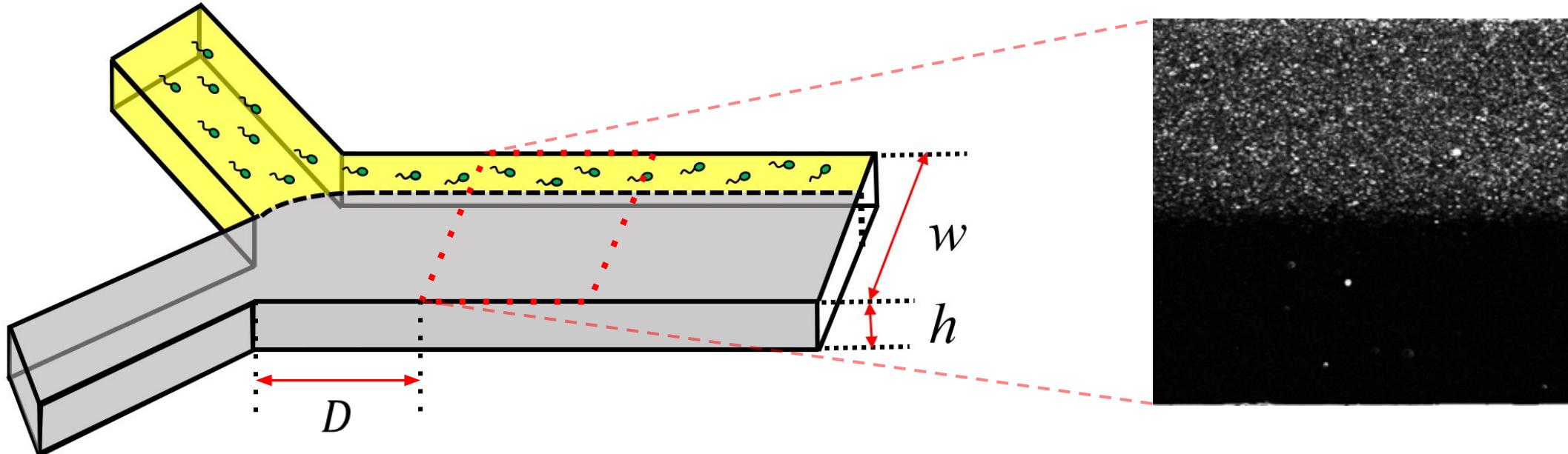
$$w = 600 \mu\text{m}$$

$$h = 25 \sim 128 \mu\text{m}$$

$$D = 500 \sim 1000 \mu\text{m}$$

$$n = 1.6 \times 10^{10} \text{ ml}^{-1}$$

# Microfluidic channel viscometer



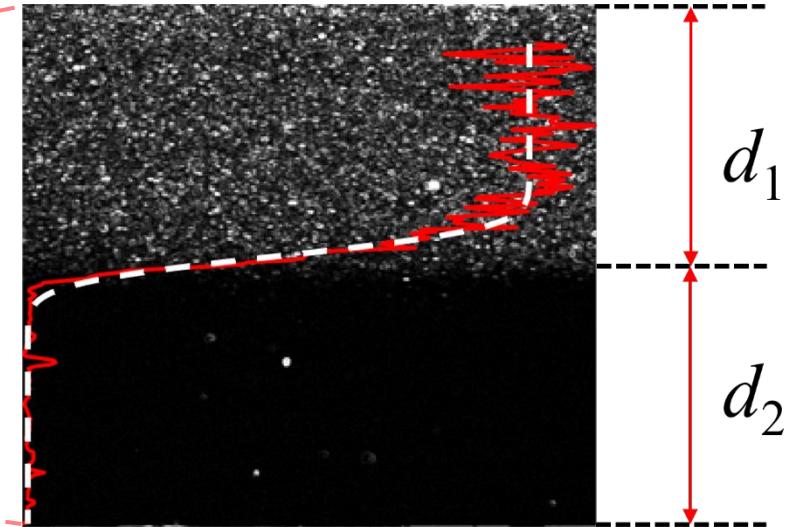
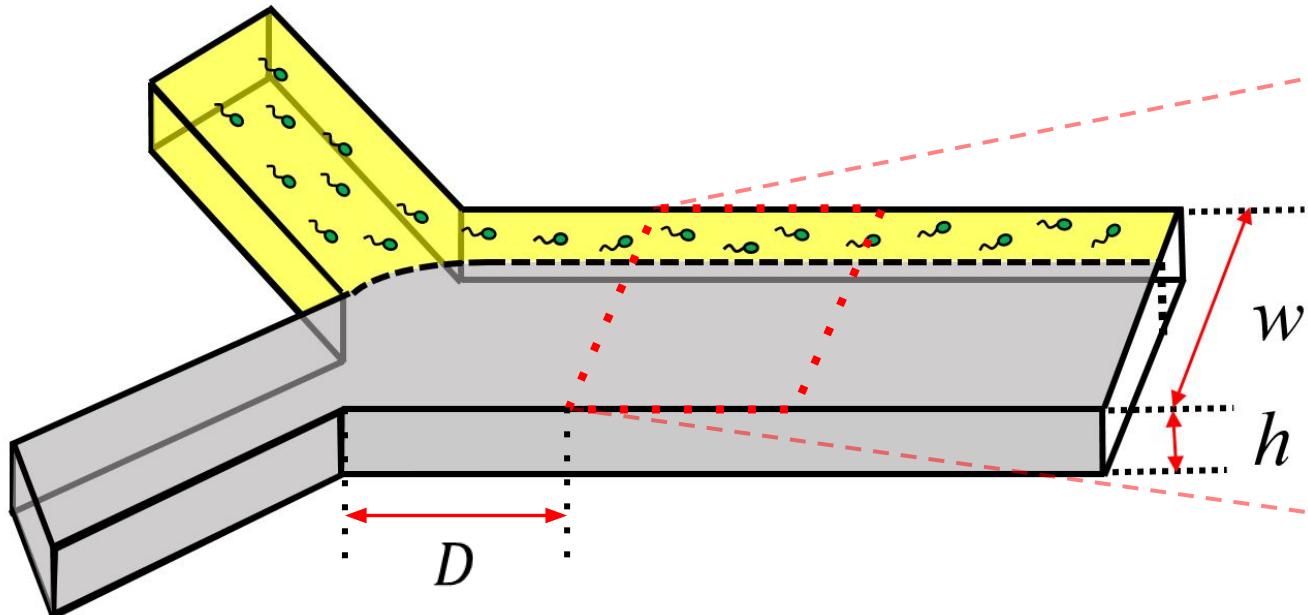
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# Microfluidic channel viscometer



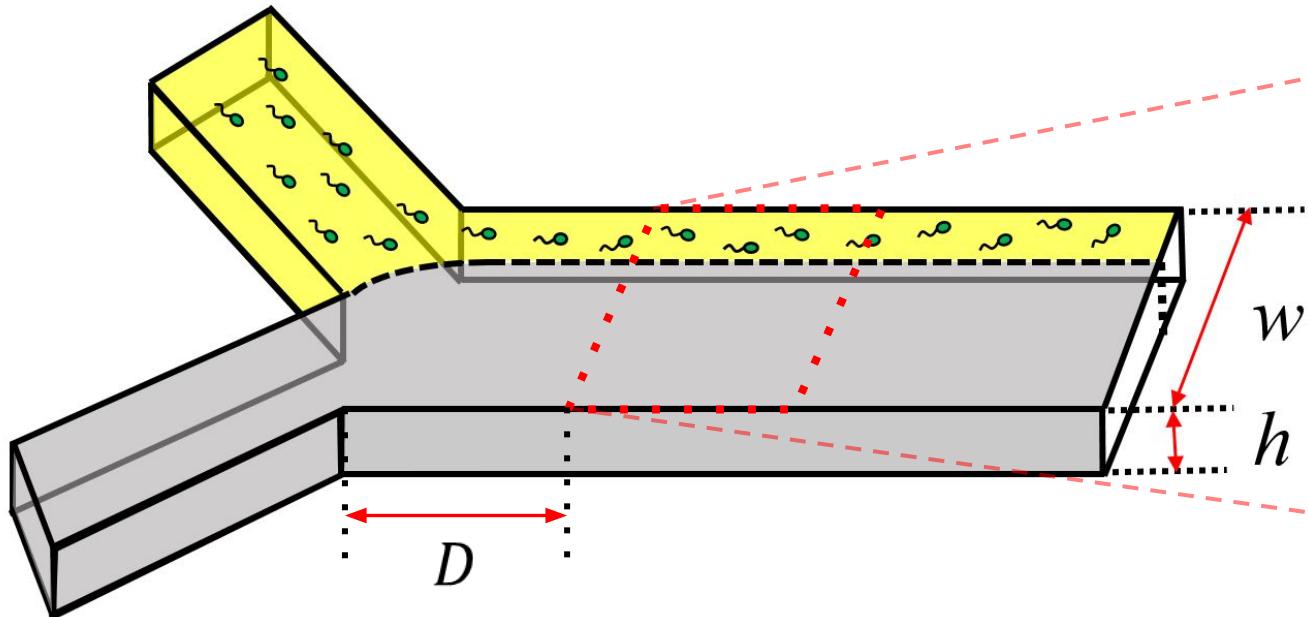
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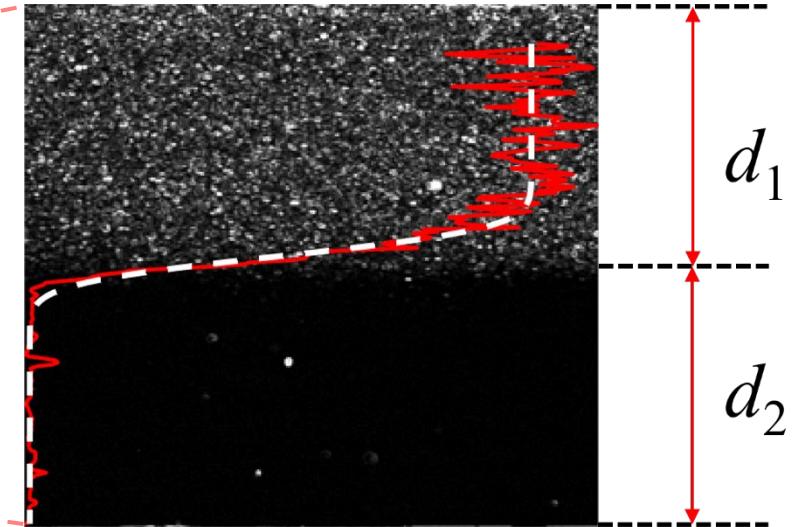


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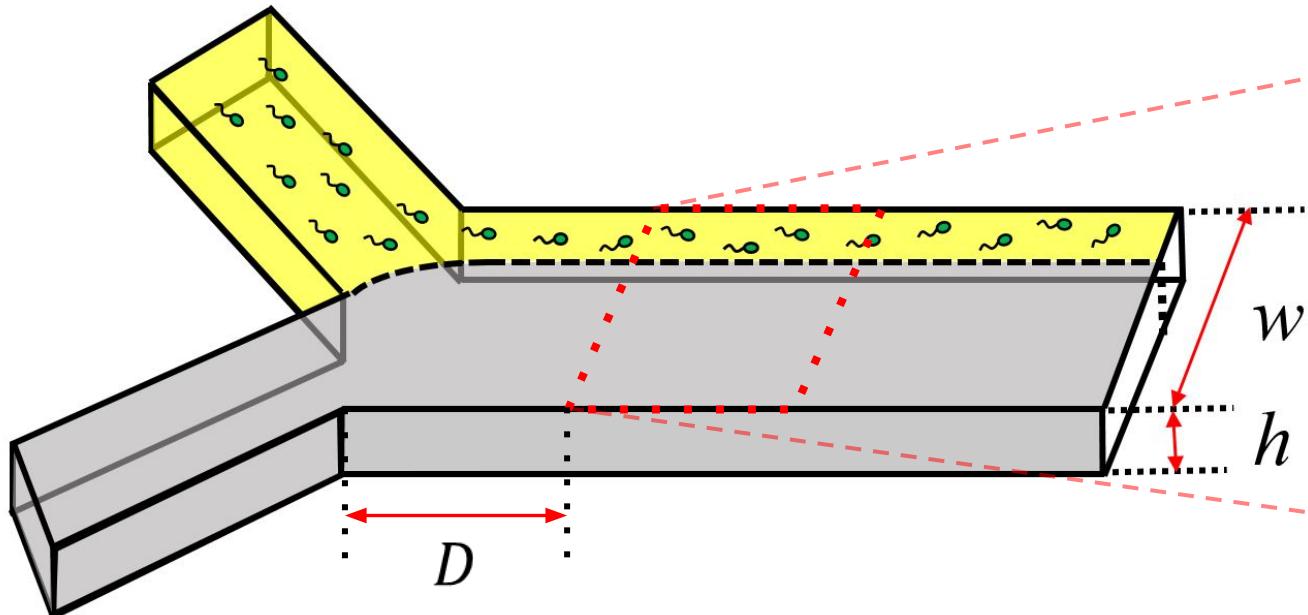
$$D = 500 \sim 1000 \mu\text{m}$$

$$n = 1.6 \times 10^{10} \text{ ml}^{-1}$$



$$\text{Relative viscosity} = \frac{\eta_1}{\eta_2} = \frac{d_1}{d_2}$$

# Microfluidic channel viscometer

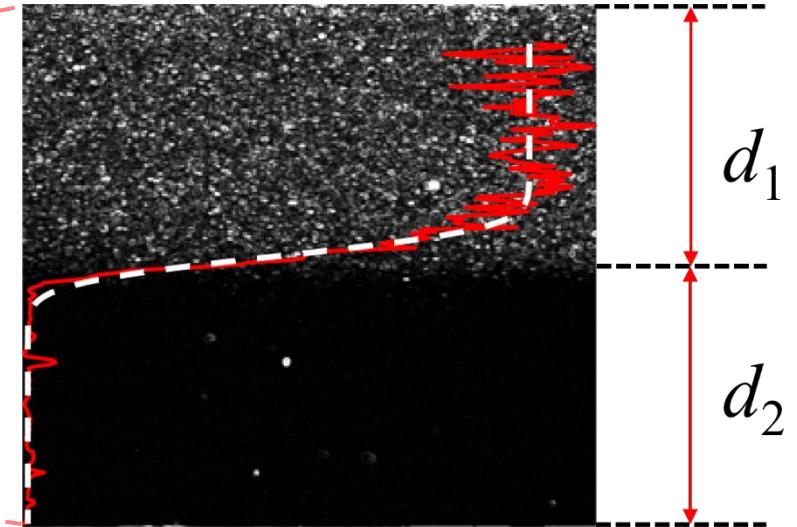


$$w = 600 \text{ } \mu\text{m}$$

$$h = 25 \sim 128 \text{ } \mu\text{m}$$

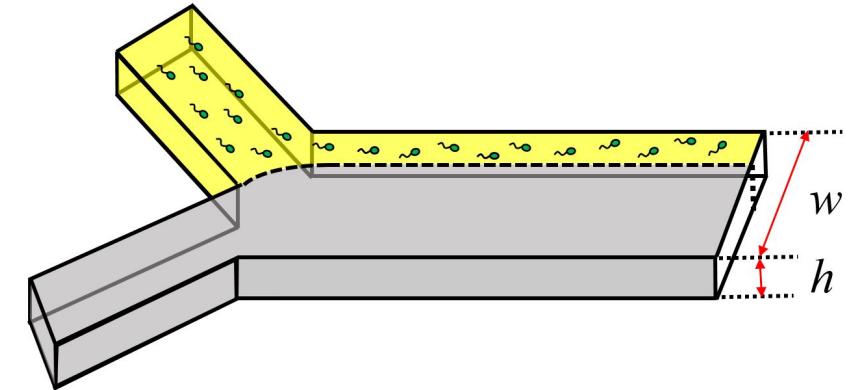
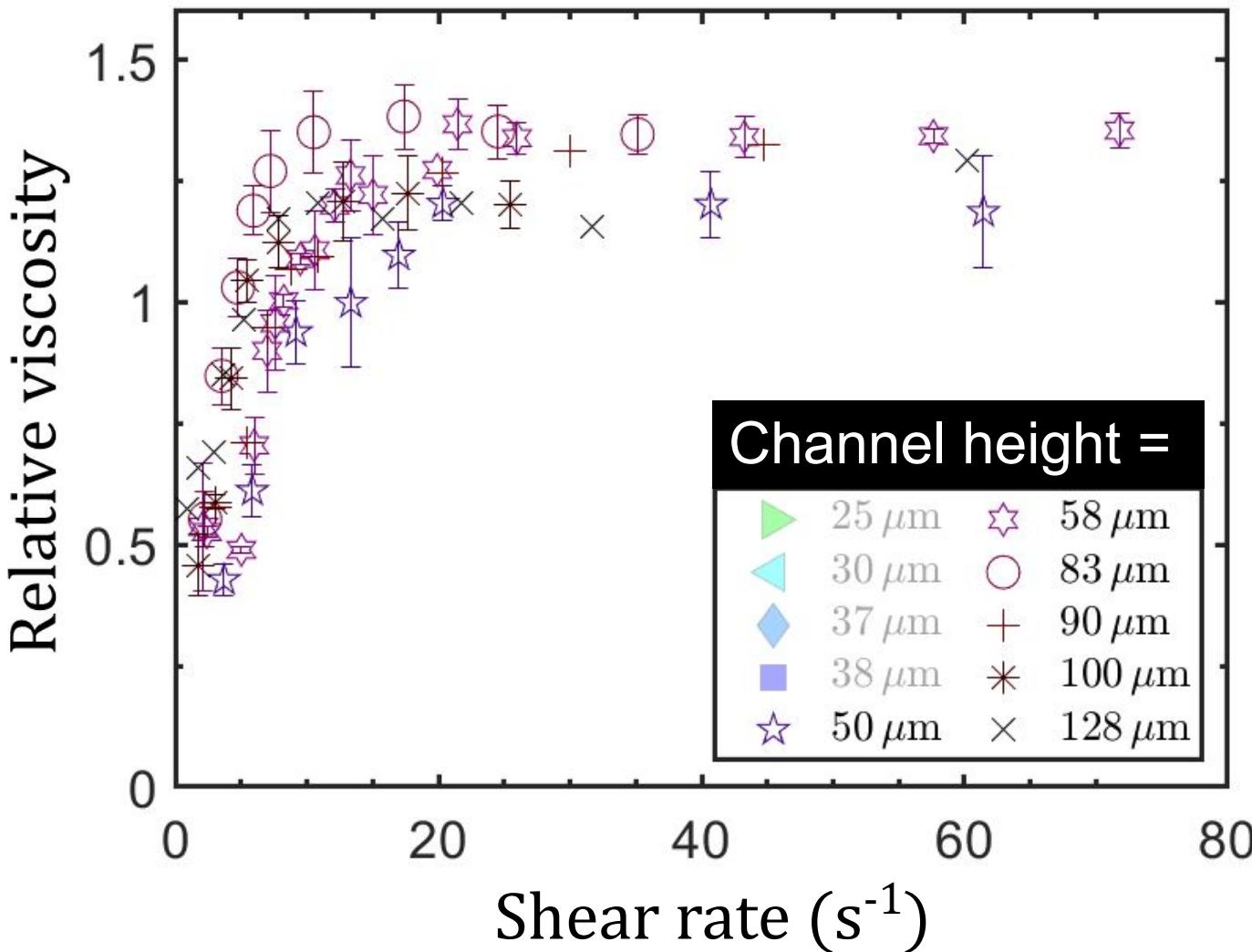
$$D = 500 \sim 1000 \text{ } \mu\text{m}$$

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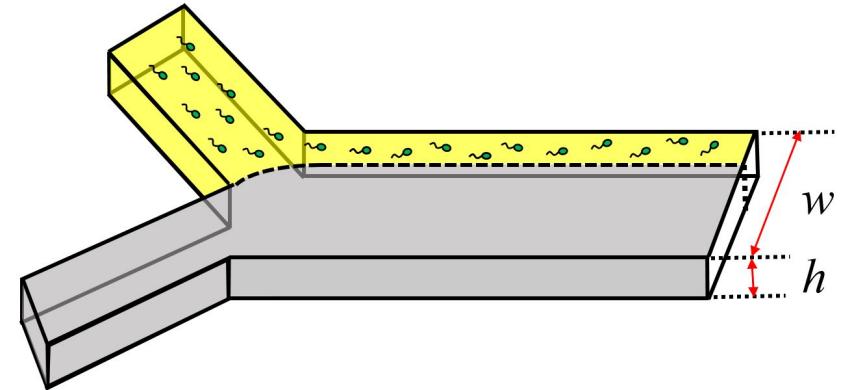
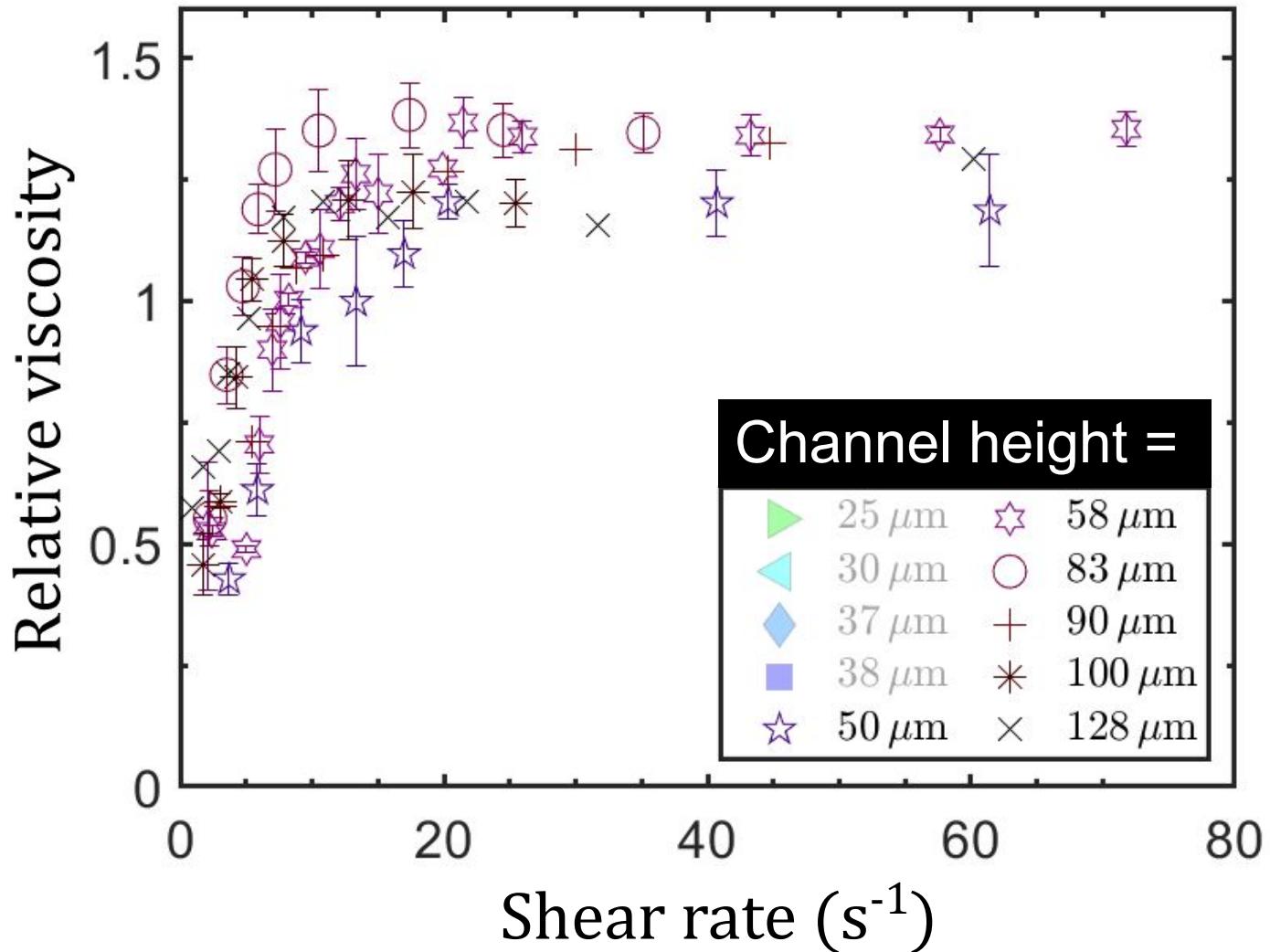
$$\text{Relative viscosity} = \frac{\eta_1}{\eta_2} = \frac{d_1}{d_2}$$

# Viscosity under confinement



$h \geq 50 \mu\text{m}$

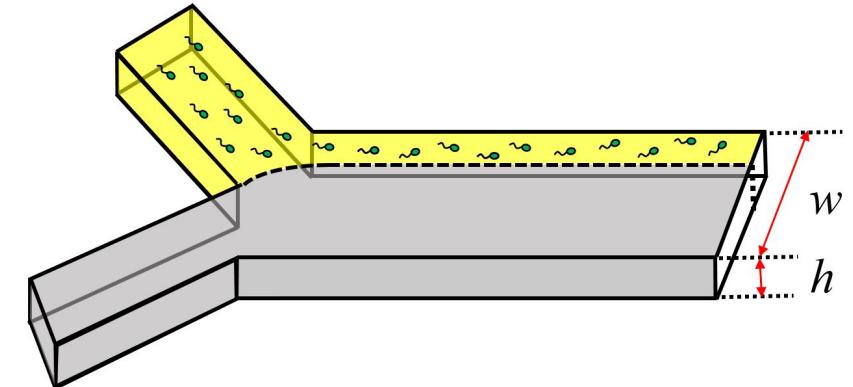
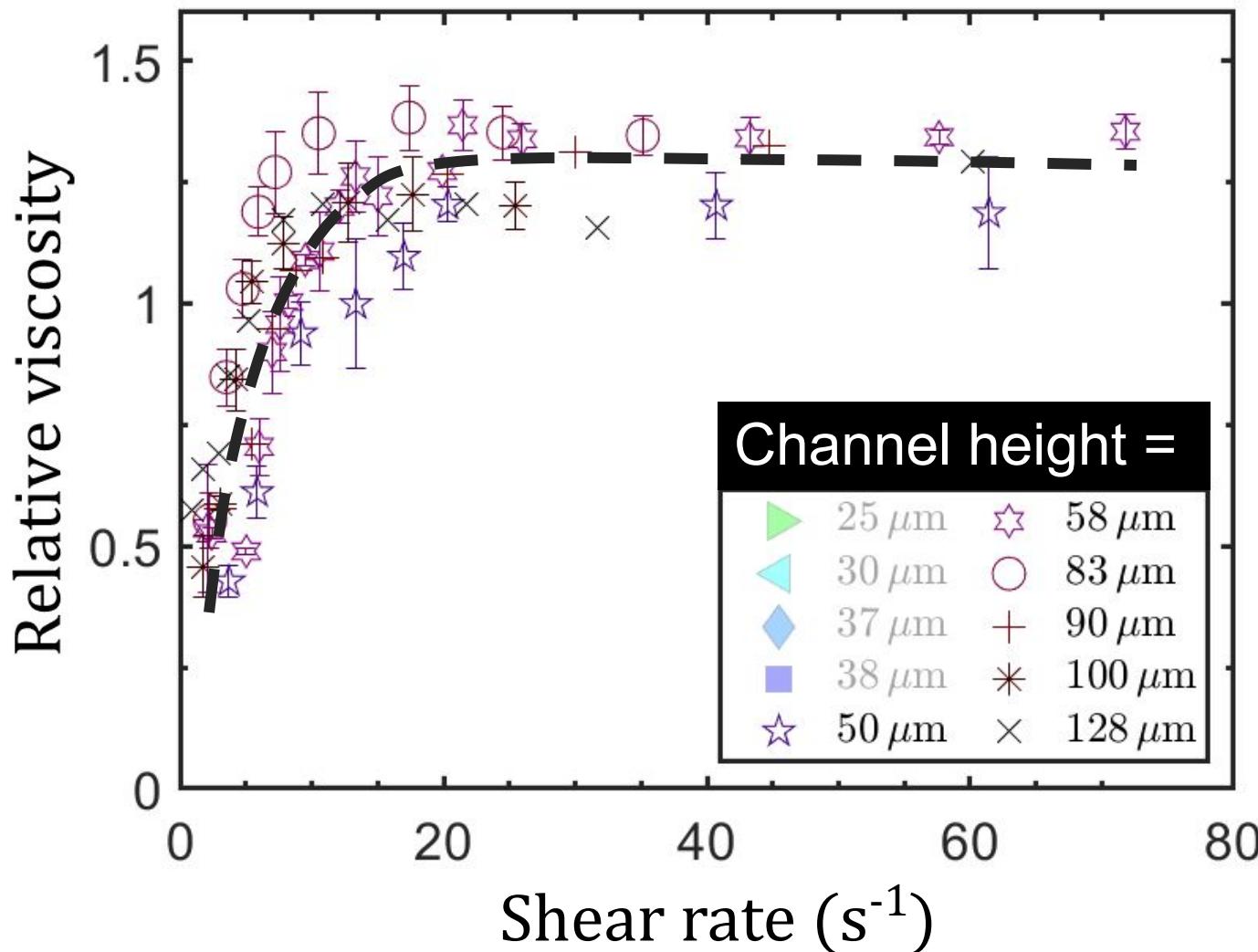
# Viscosity under confinement



$$h \geq 50 \mu\text{m}$$

- Viscosity reduction at low shear rate

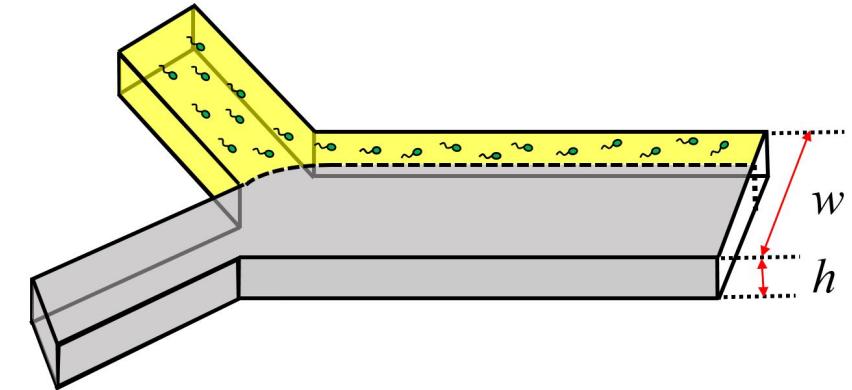
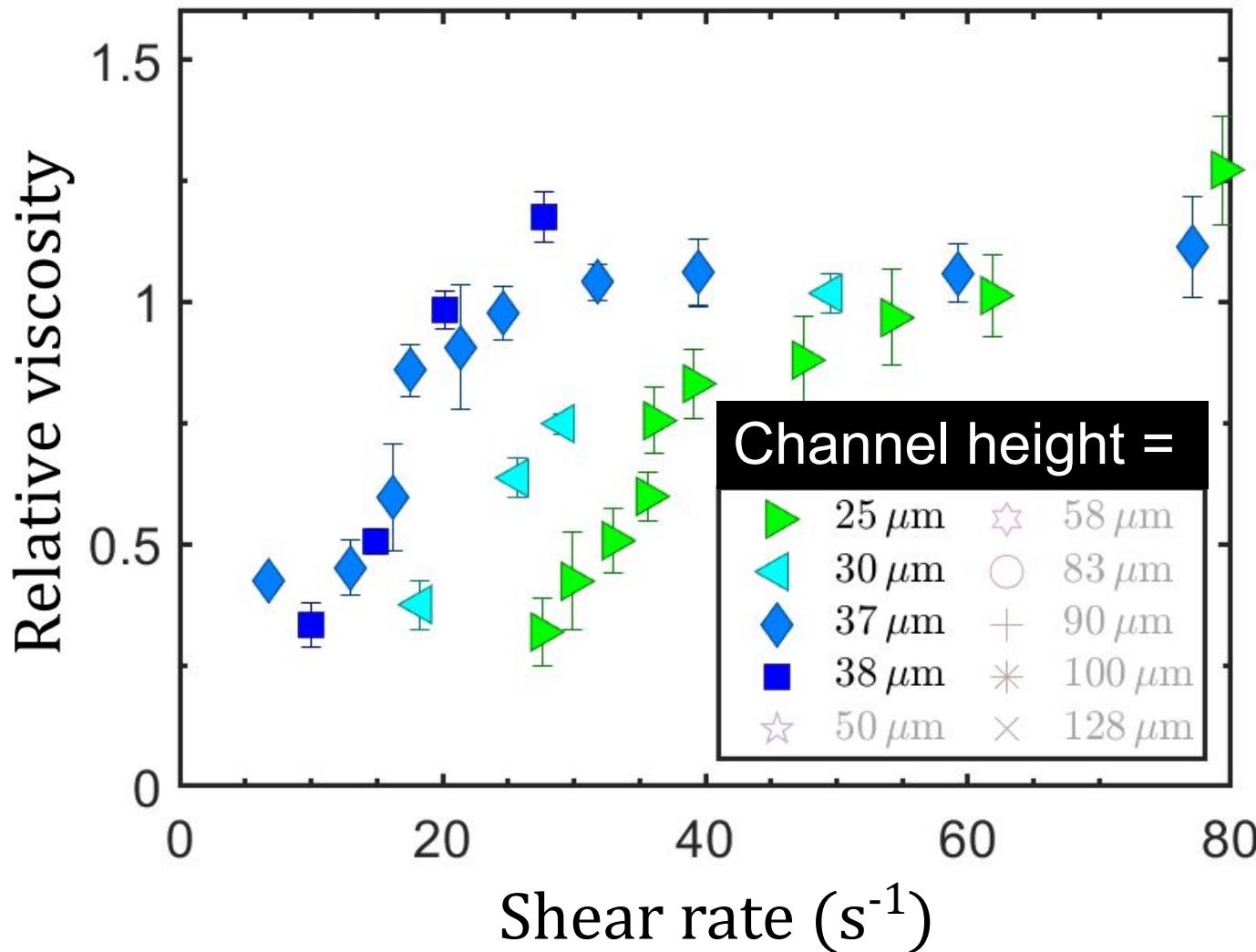
# Viscosity under confinement



$$h \geq 50 \mu\text{m}$$

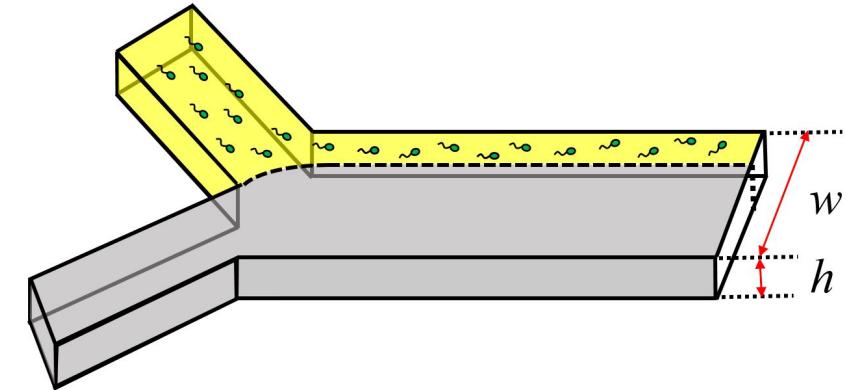
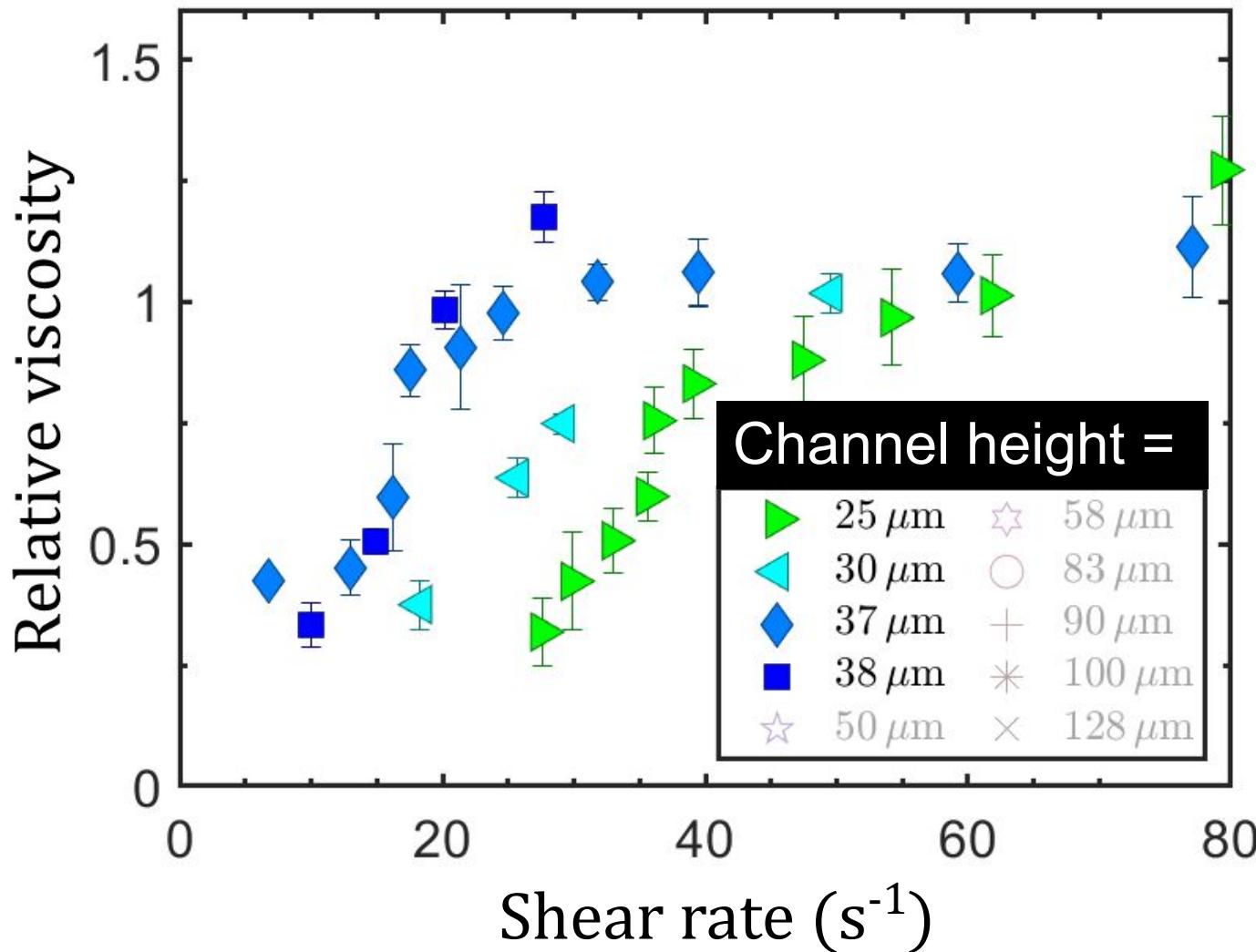
- Viscosity reduction at low shear rate
- Fall on a same master curve: no confinement effect

# Viscosity under confinement



$h < 50 \mu\text{m}$

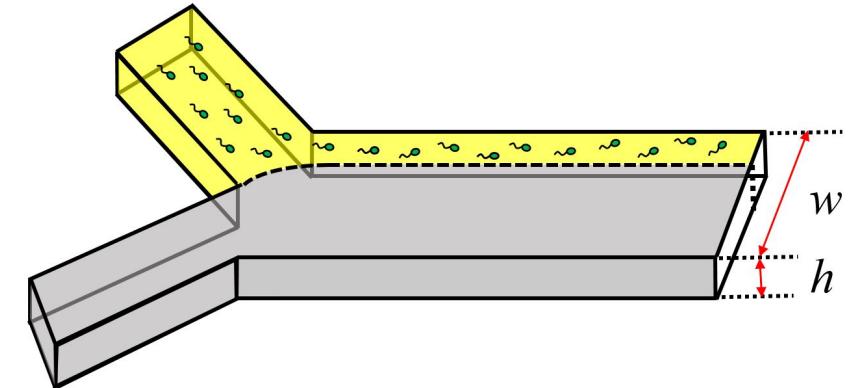
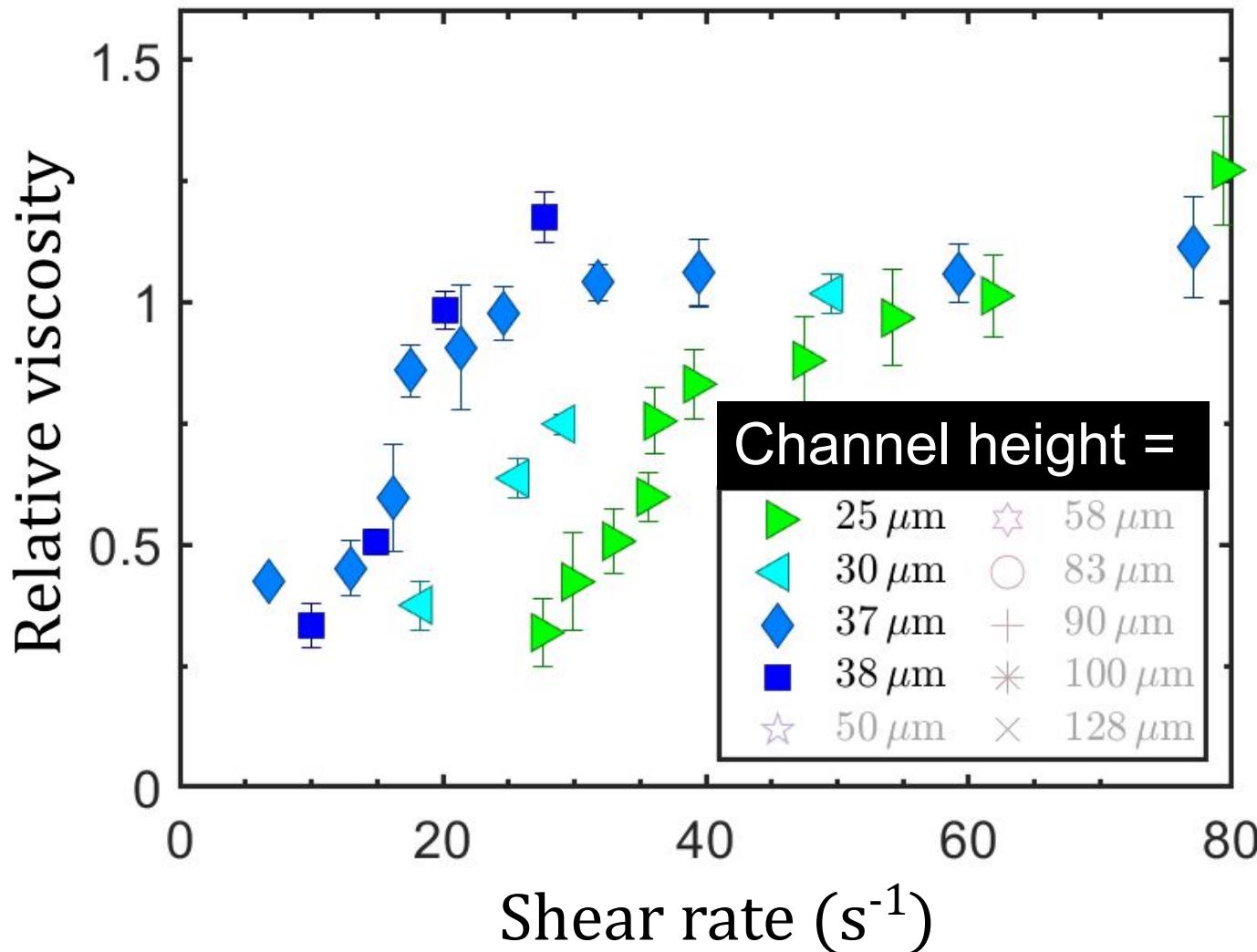
# Viscosity under confinement



$h < 50 \mu\text{m}$

- Viscosity reduction at low shear rate

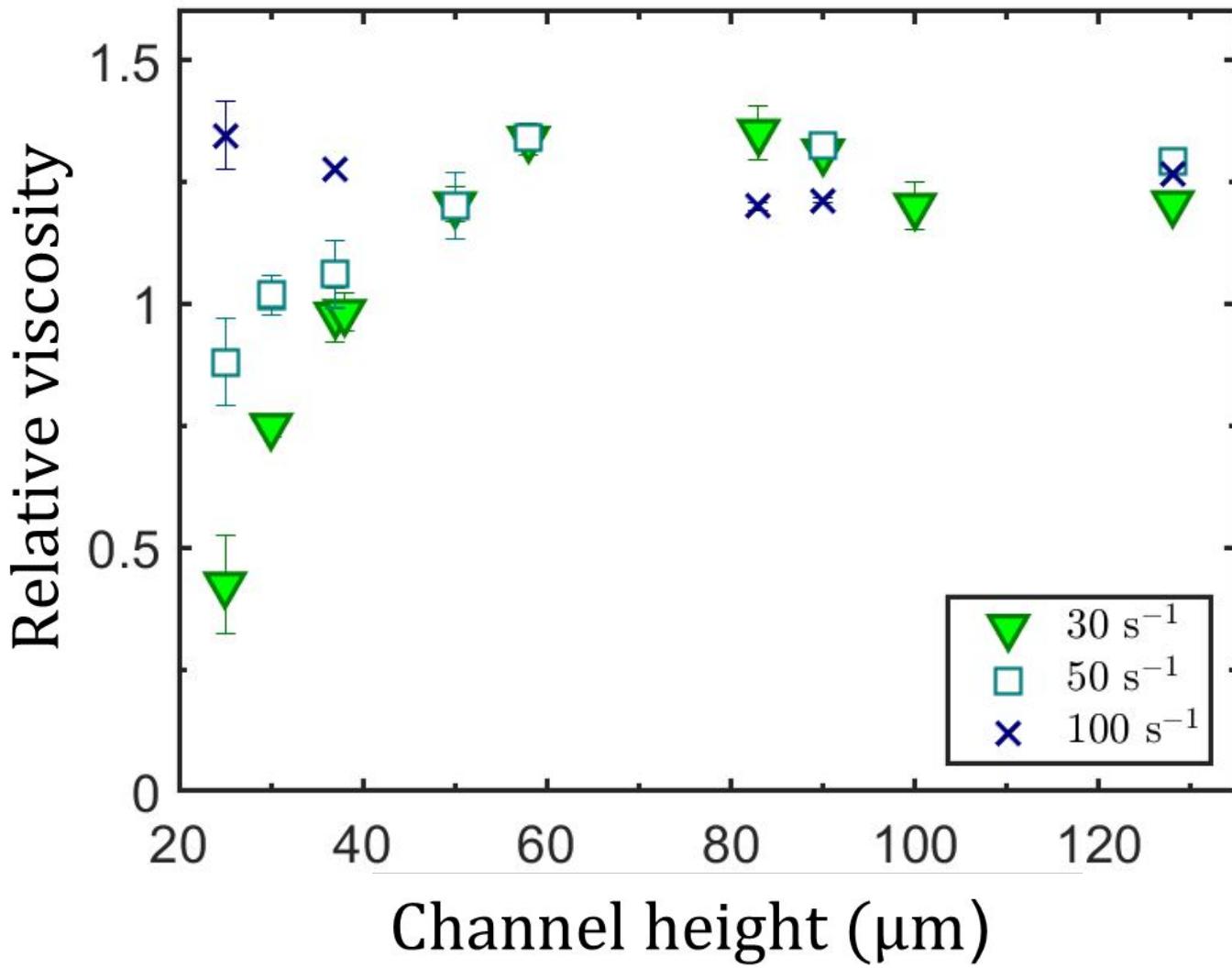
# Viscosity under confinement



$$h < 50 \mu\text{m}$$

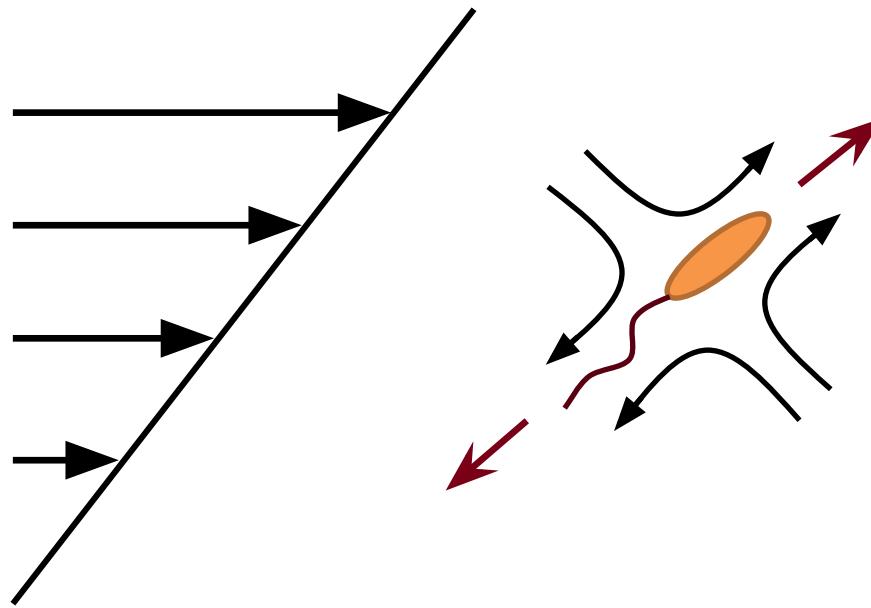
- Viscosity reduction at low shear rate
- Separated: a sign of confinement effect

# Viscosity under confinement

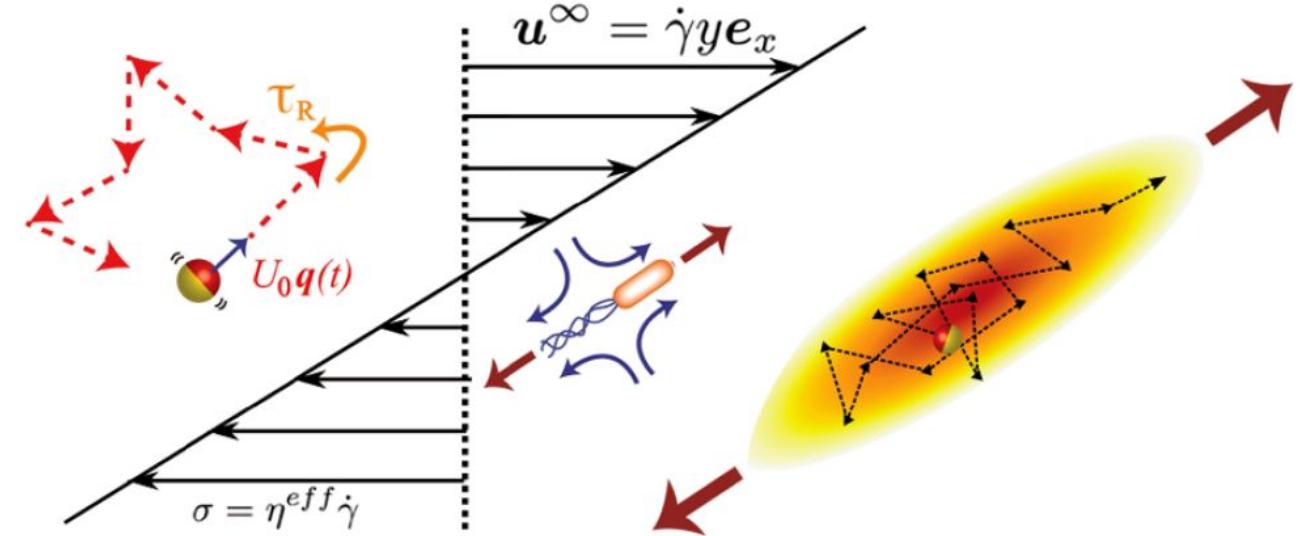


- At low shear rate, confinement **reduces** viscosity
- At high shear rate, viscosity is **independent** of confinement

# Existing mechanisms for bulk suspensions



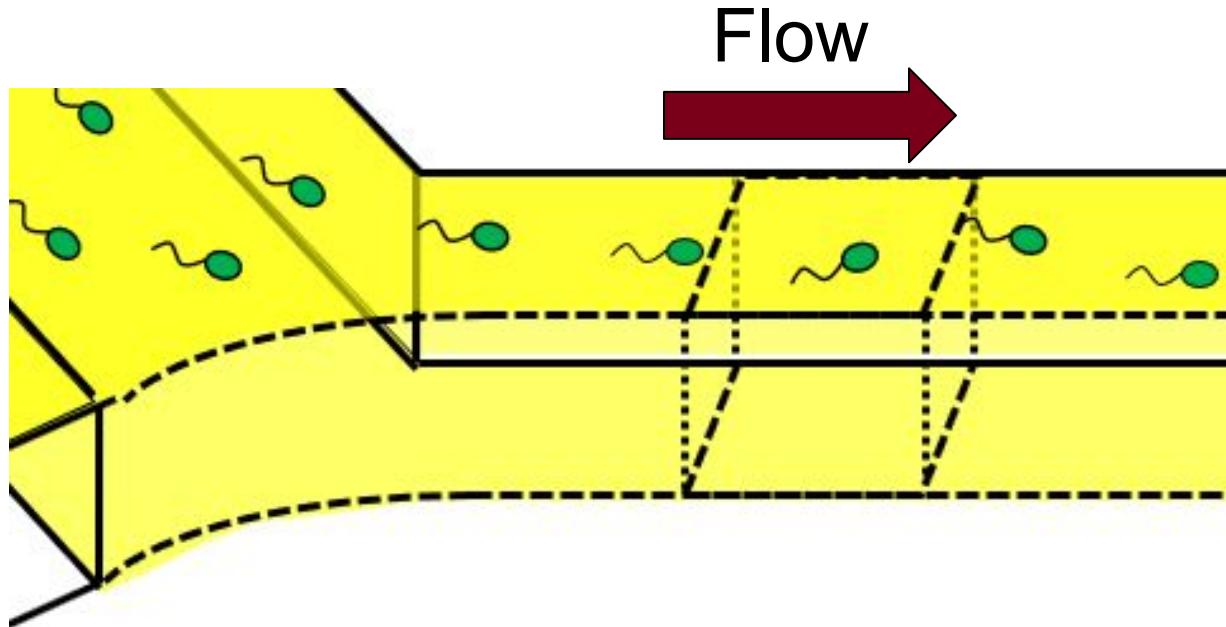
hydrodynamic stress



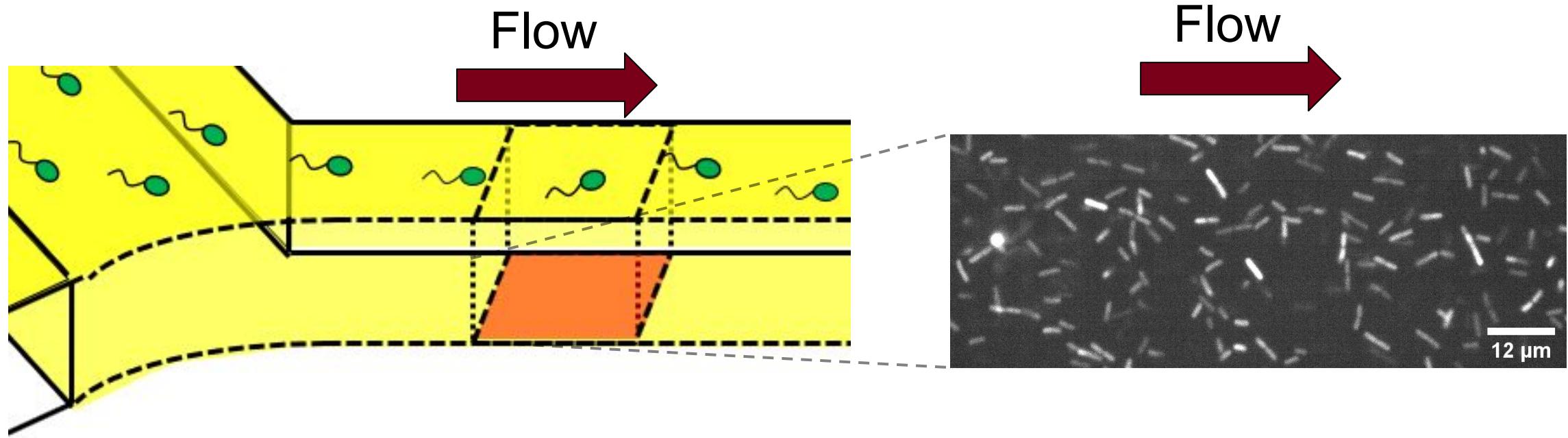
$$\sigma_{xy}^{\text{swim}} = -n\zeta D_{xy}^{\text{swim}}$$

swim stress

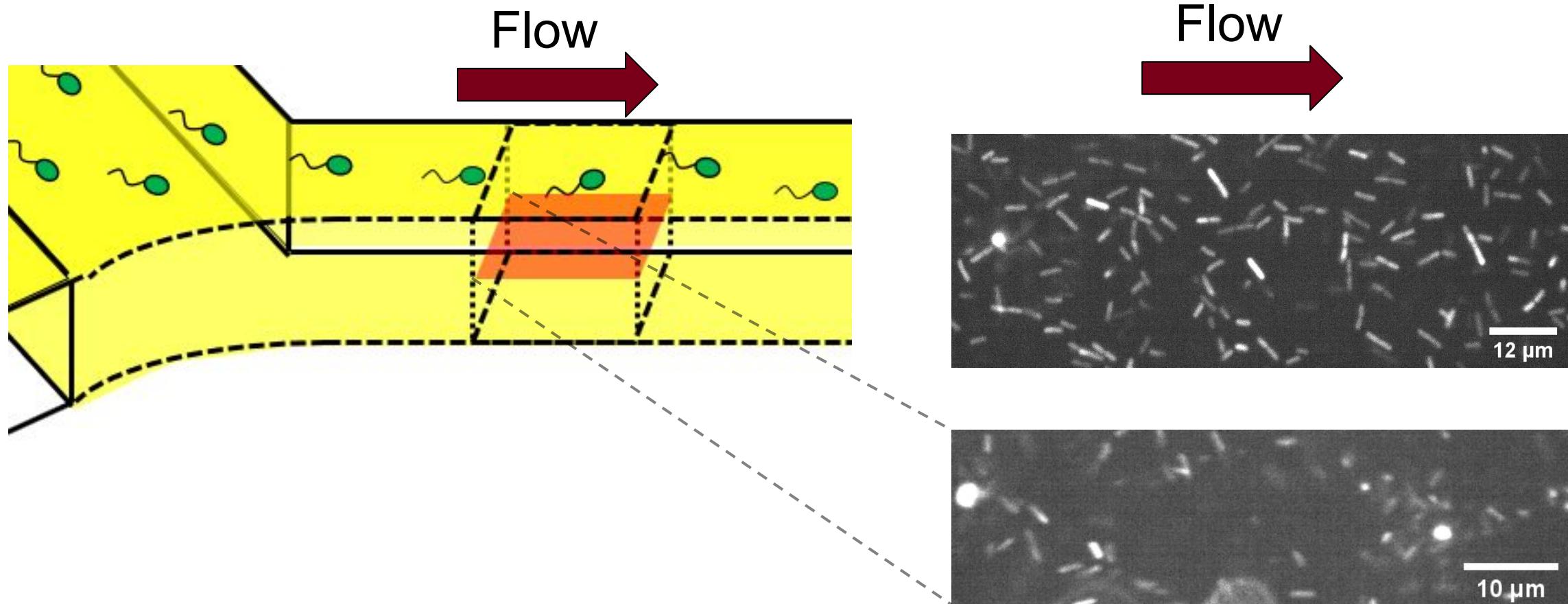
# Relative motion near boundary



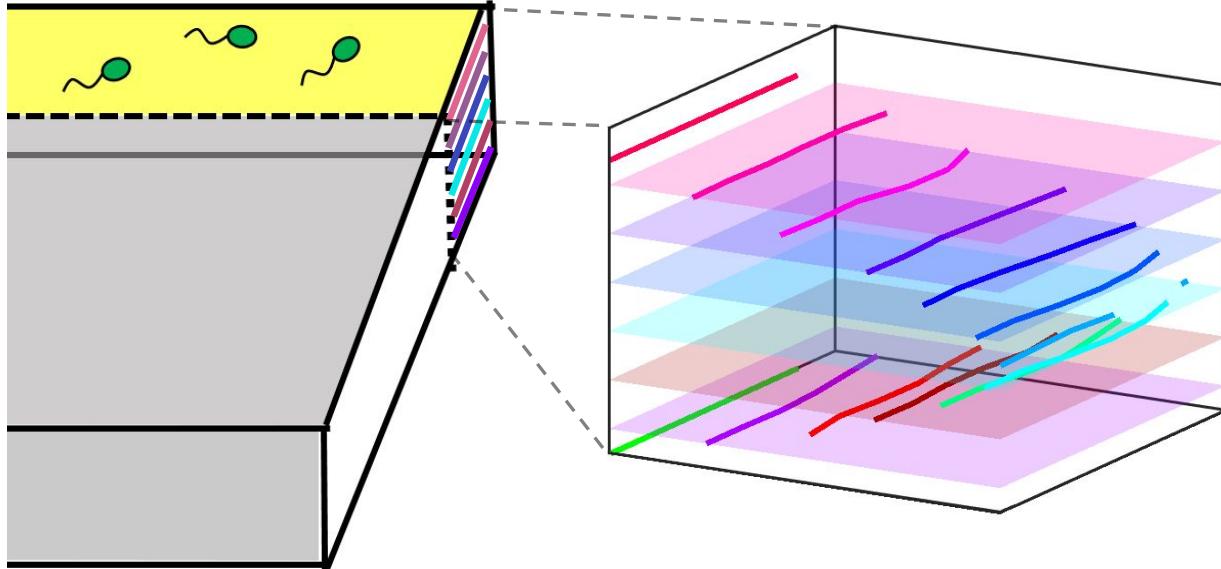
# Relative motion near boundary



# Relative motion near boundary

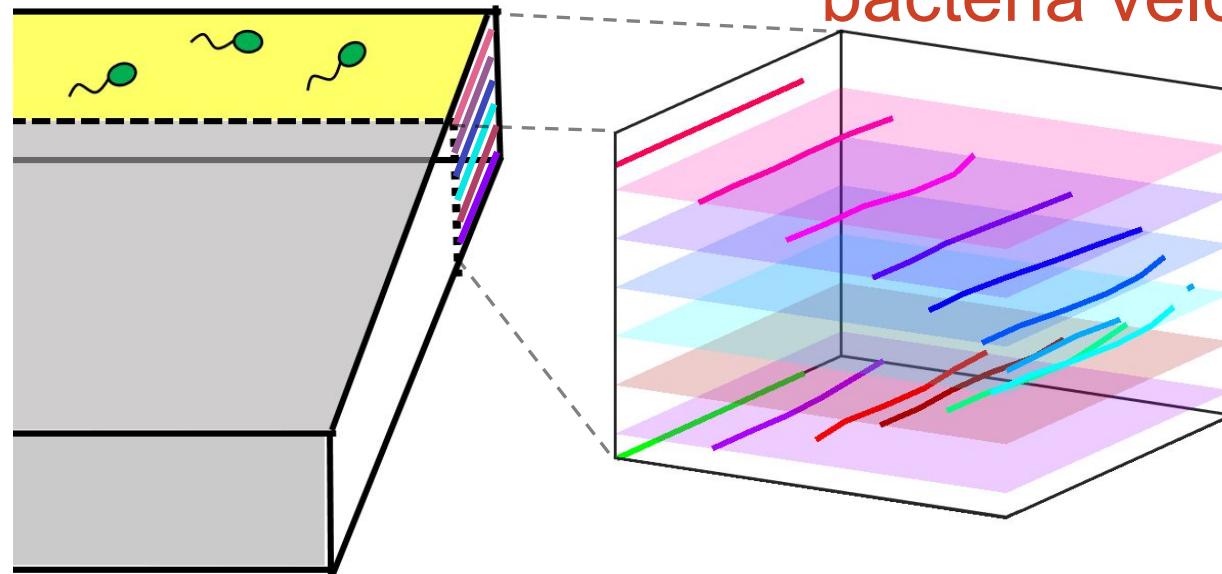


# Velocity profile



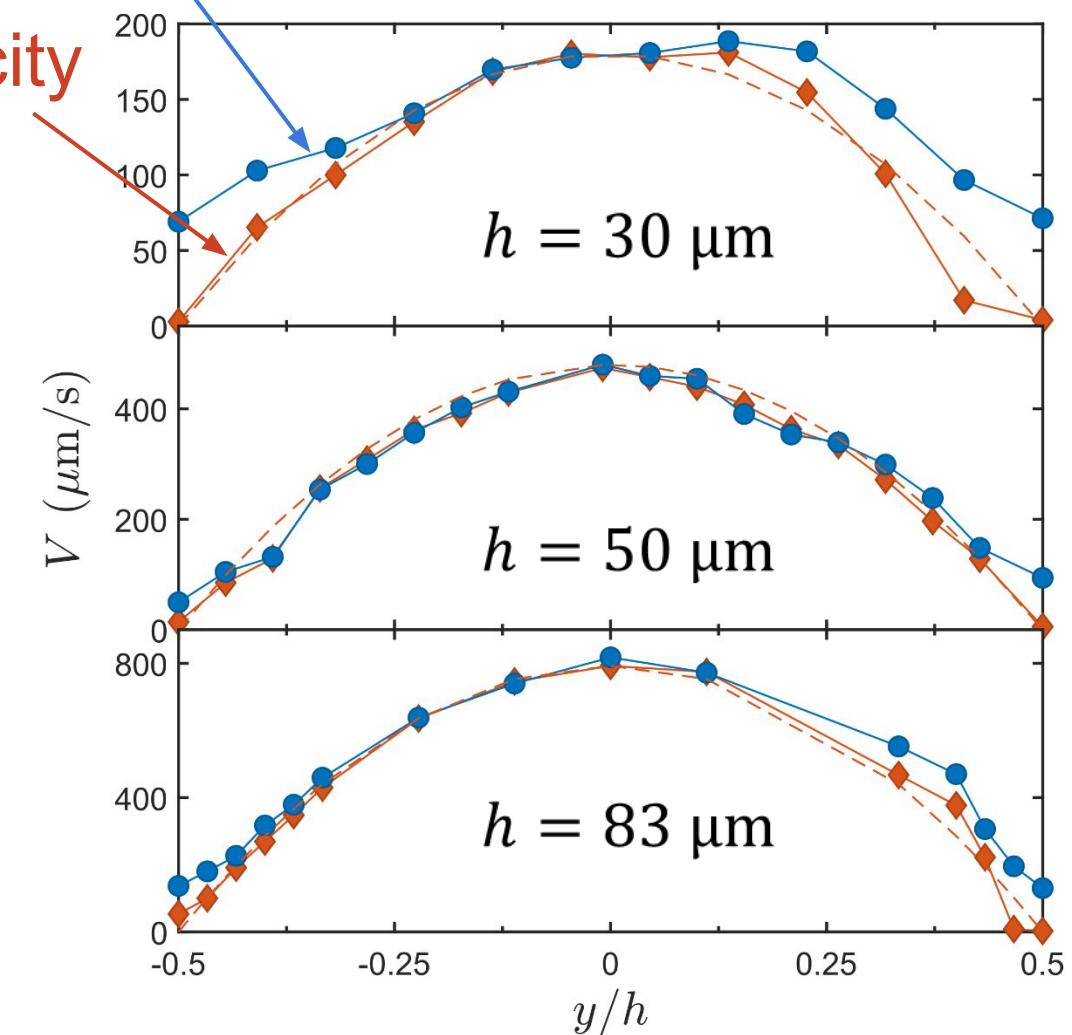
Get velocity profile by imaging layer by layer using confocal microscopy

# Velocity profile

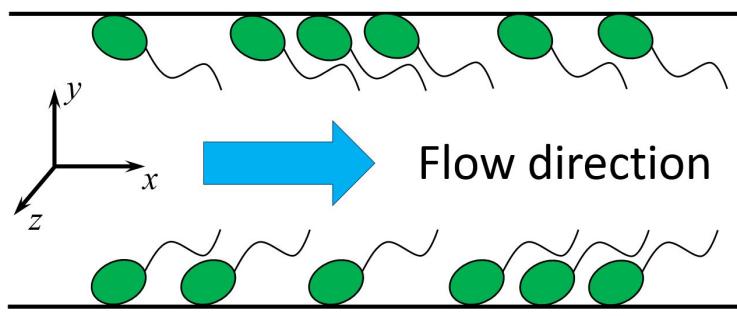


Get velocity profile by imaging layer by layer using confocal microscopy

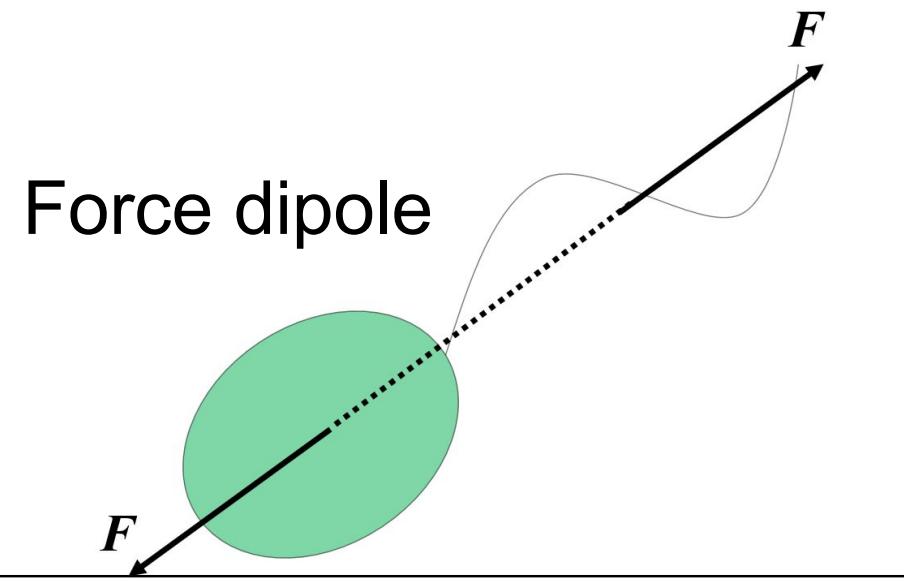
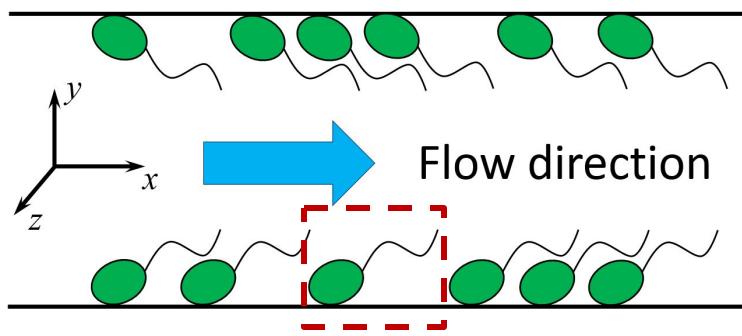
tracer velocity  
Shear rate =  $30 \text{ s}^{-1}$



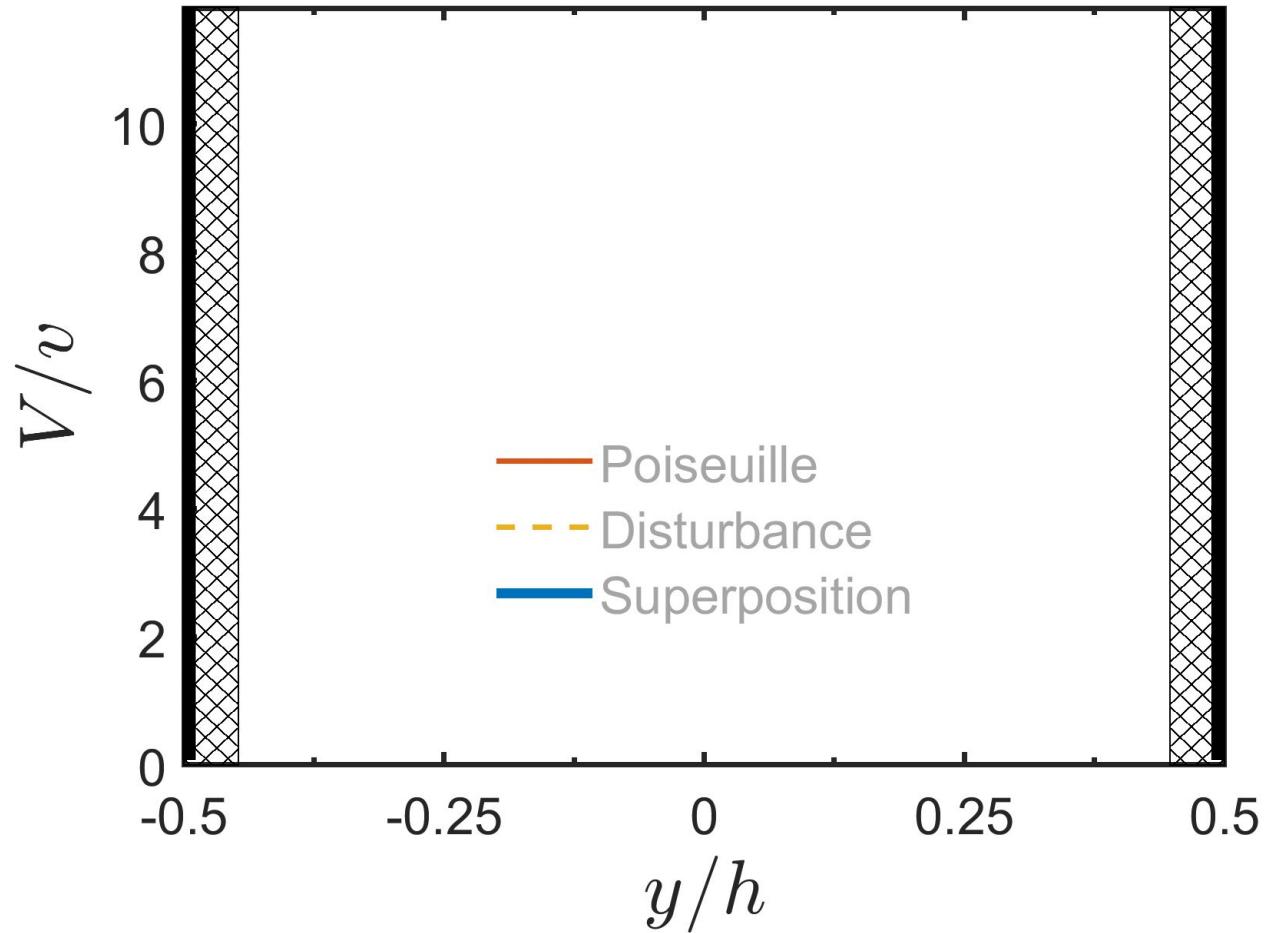
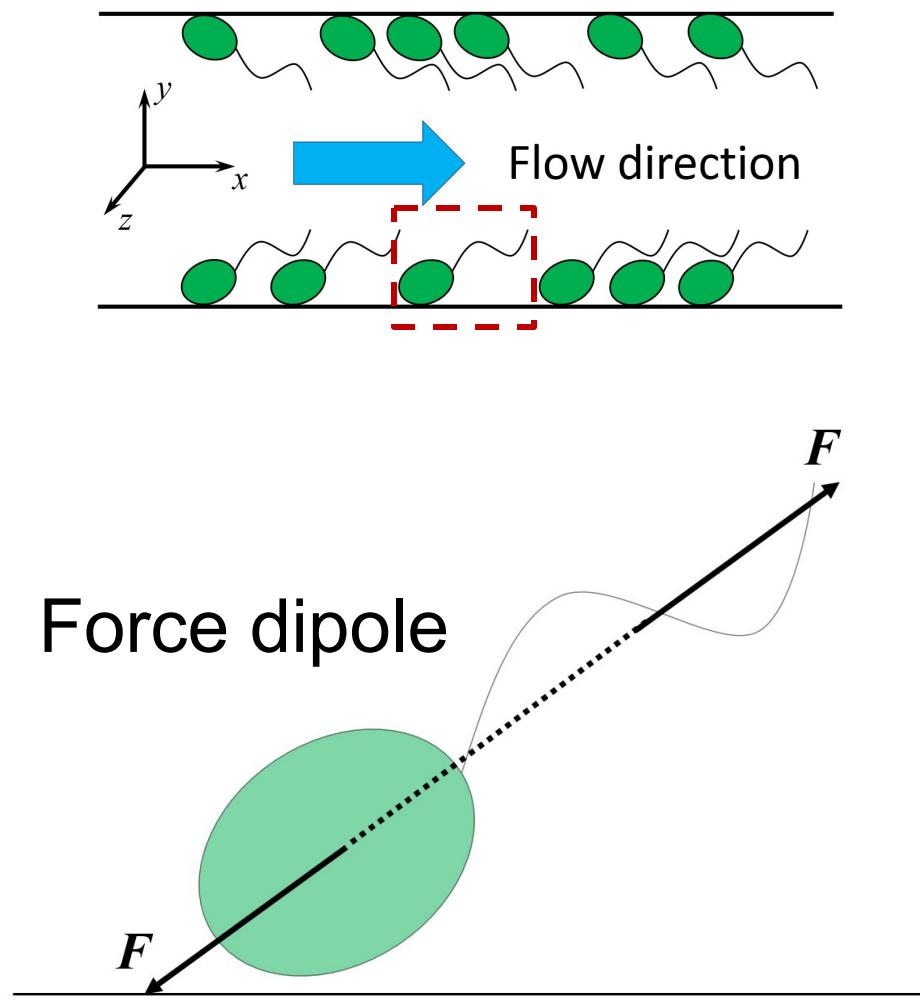
# Boundary bacteria push fluid forward



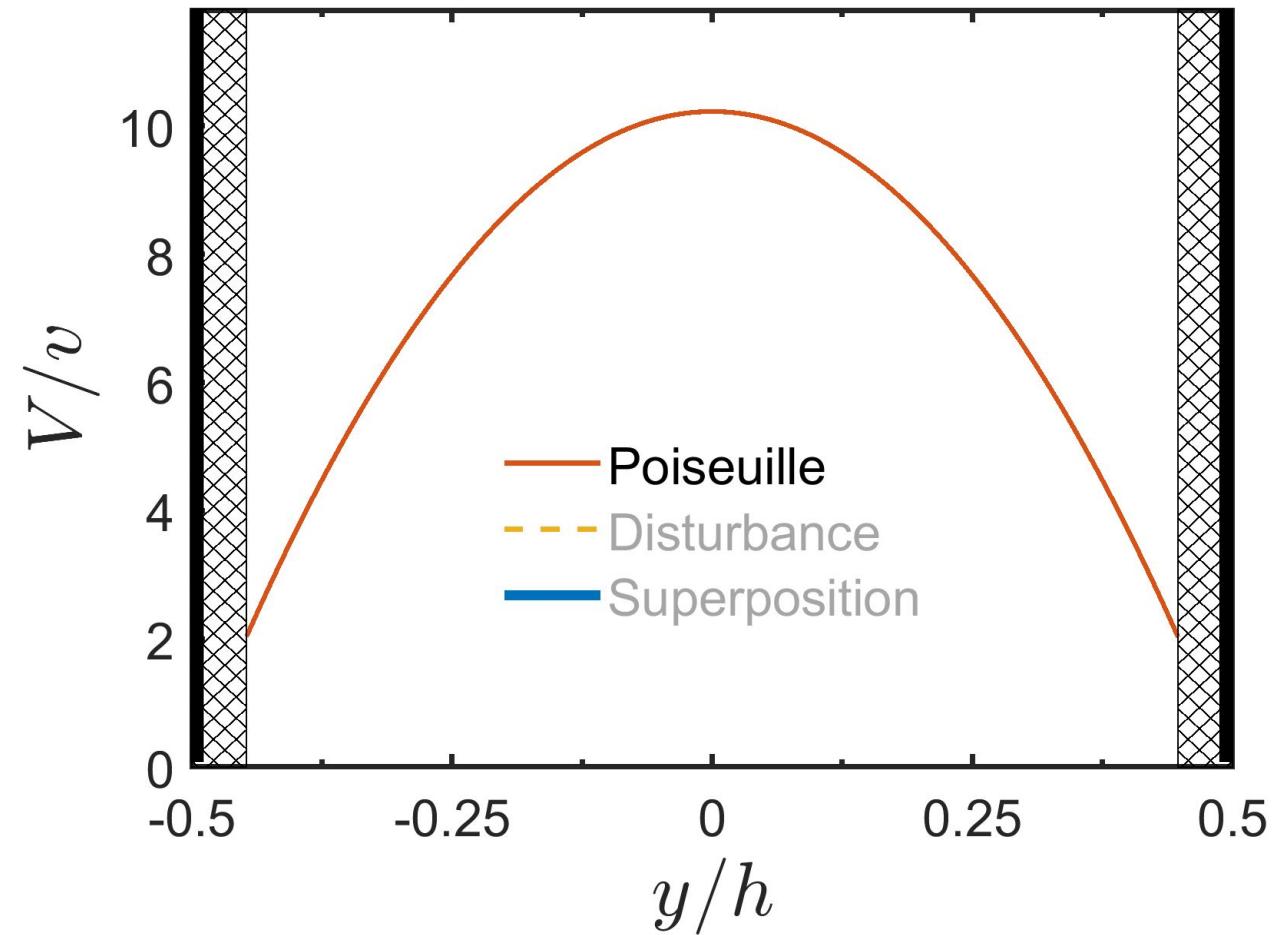
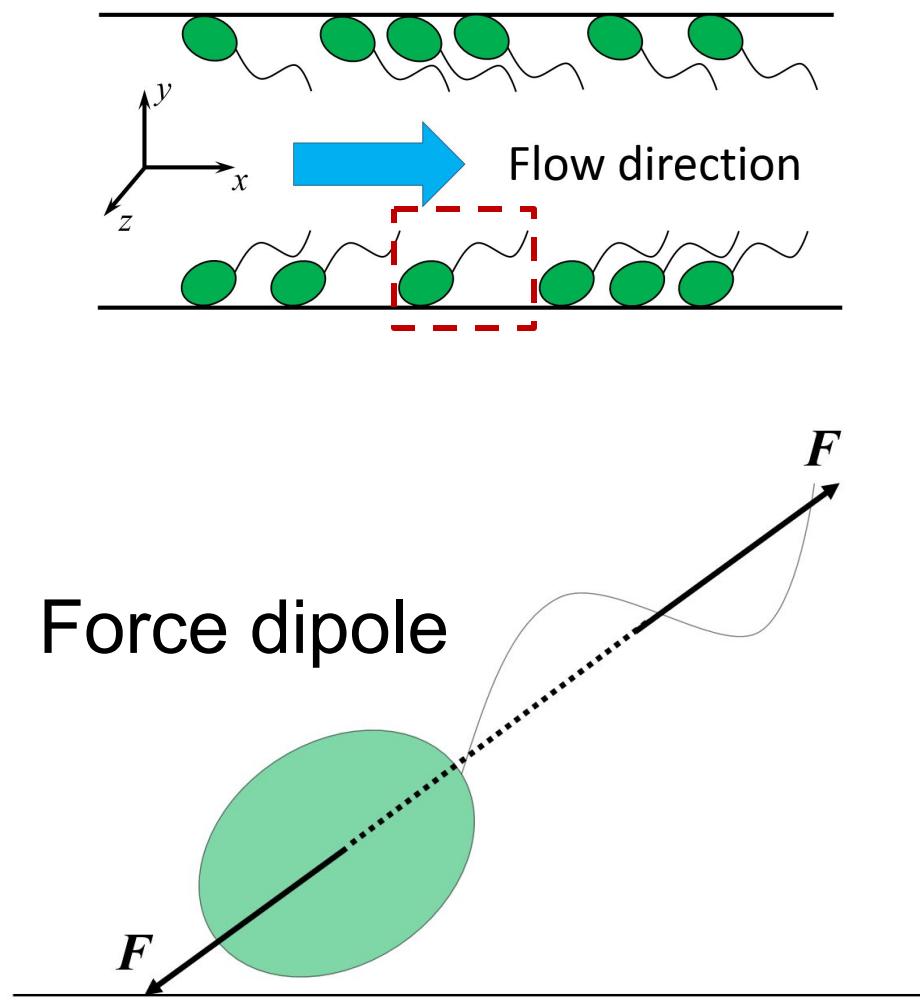
# Boundary bacteria push fluid forward



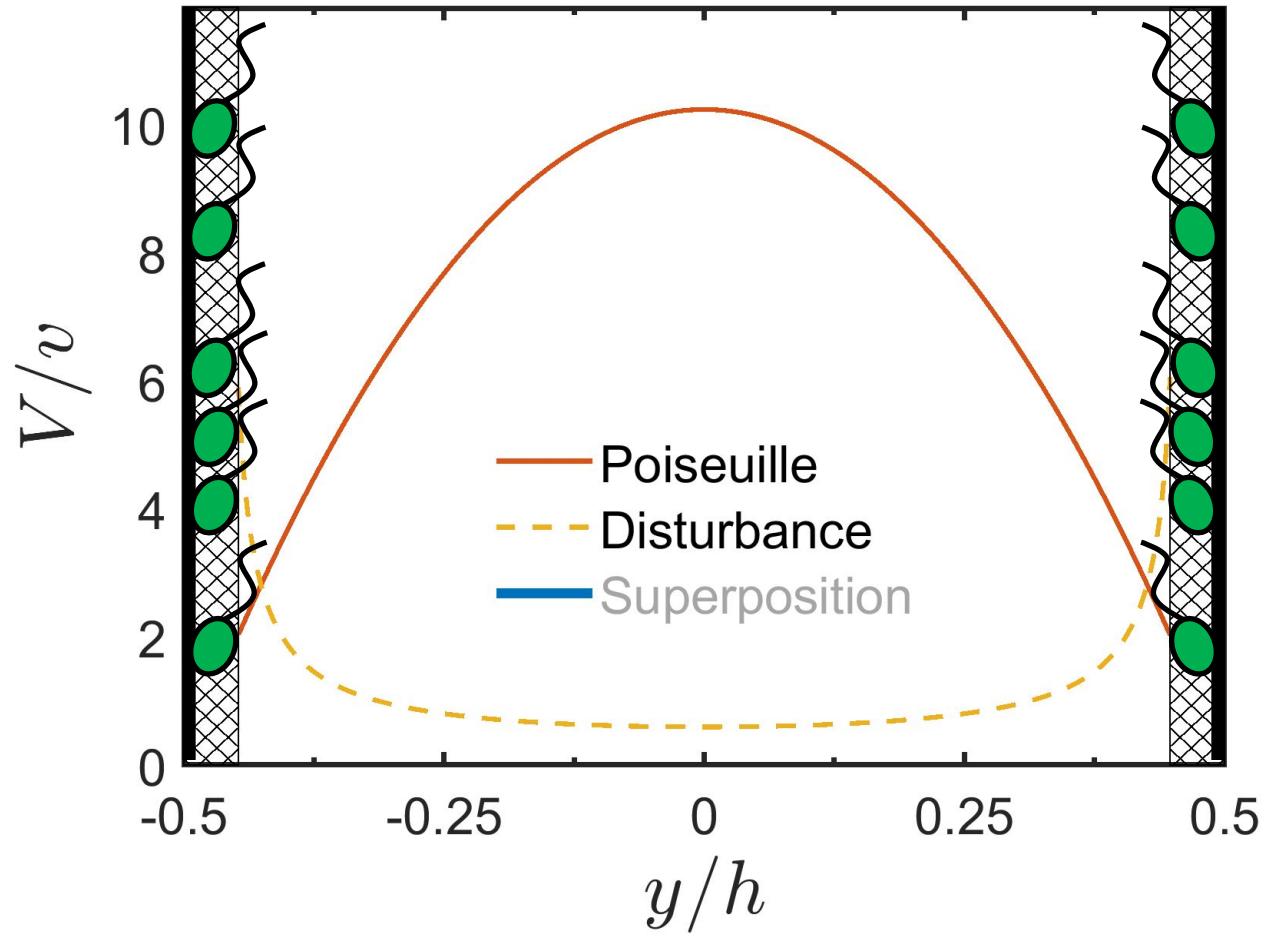
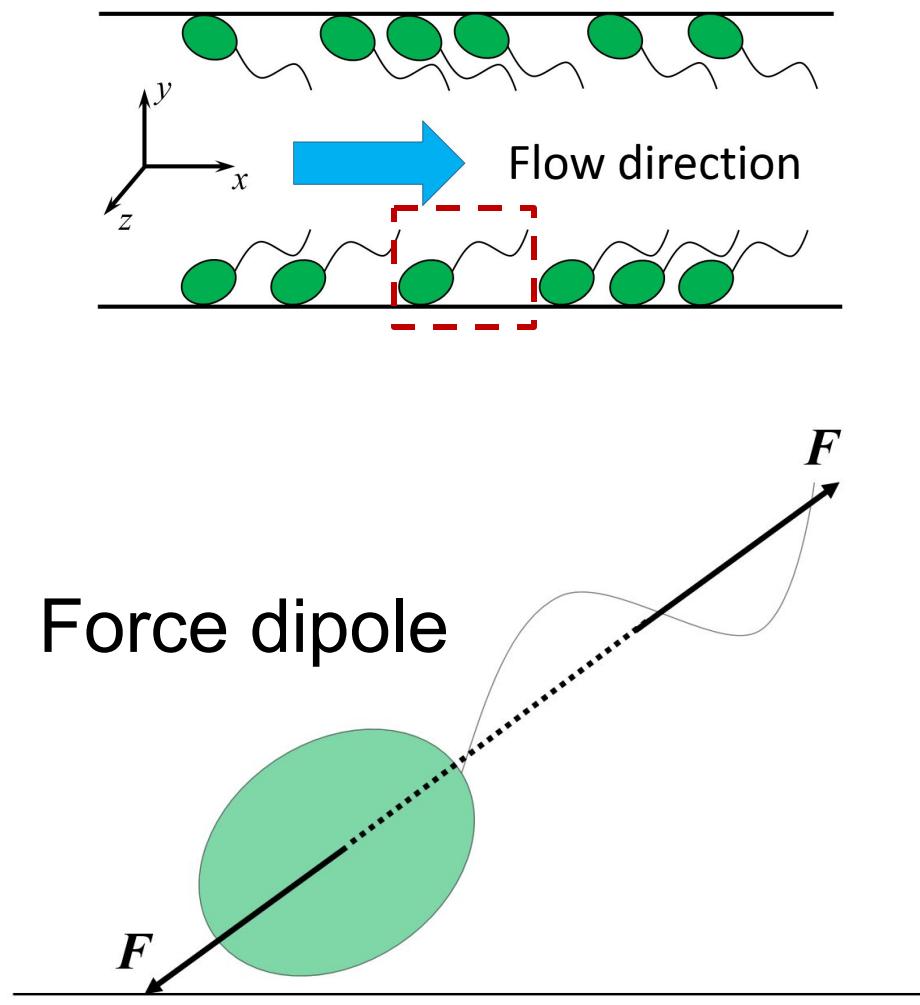
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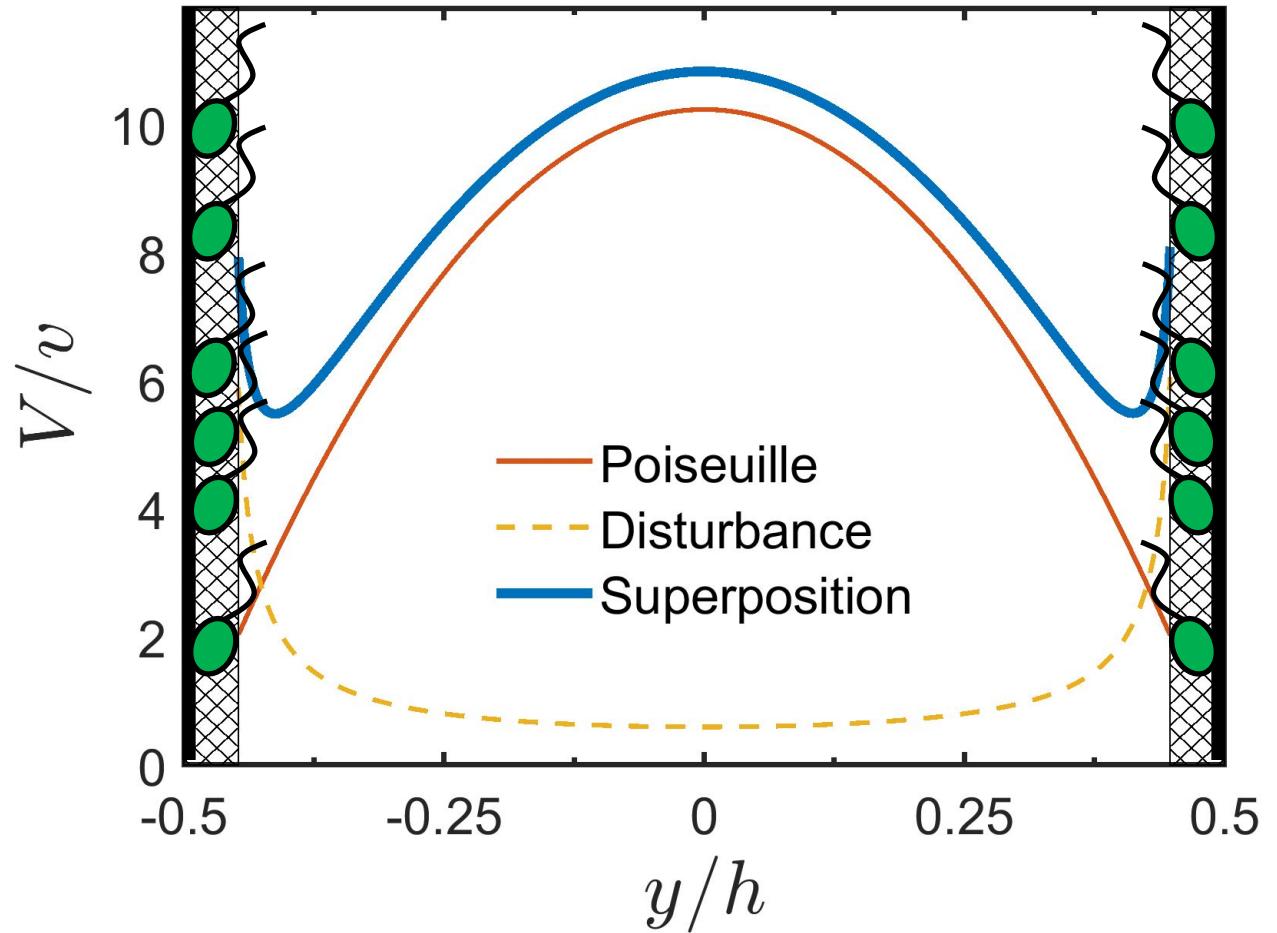
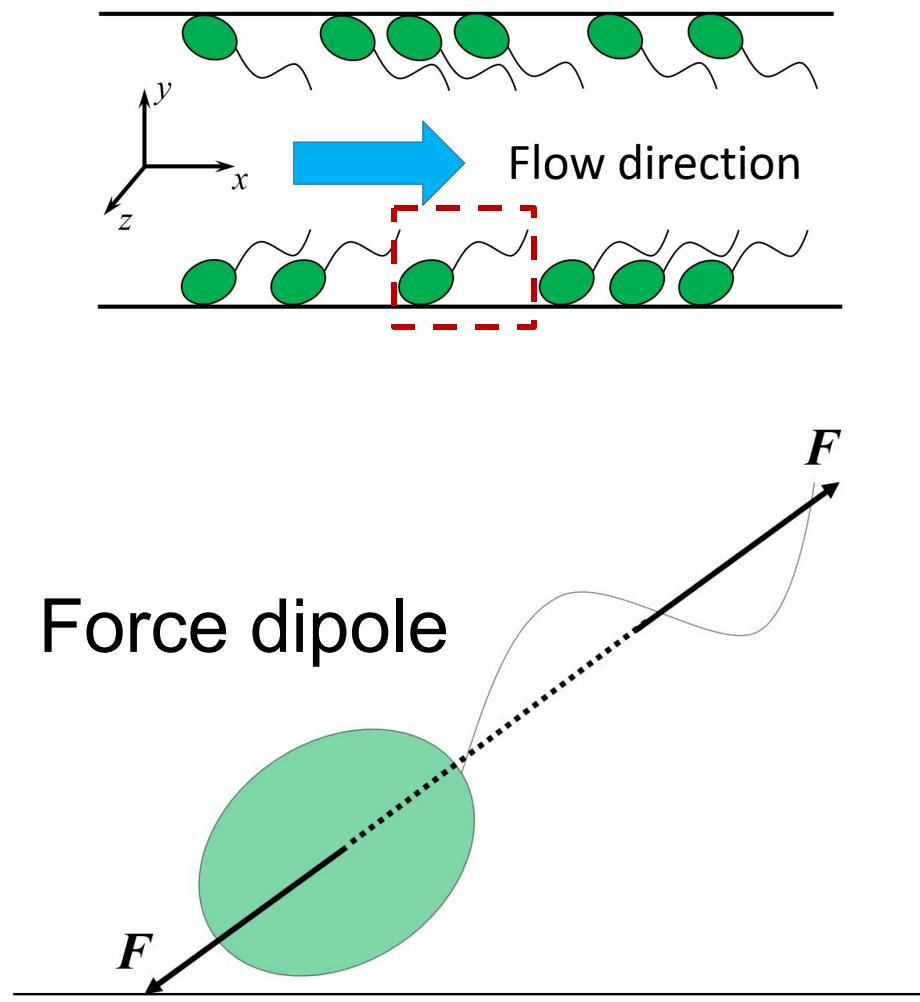
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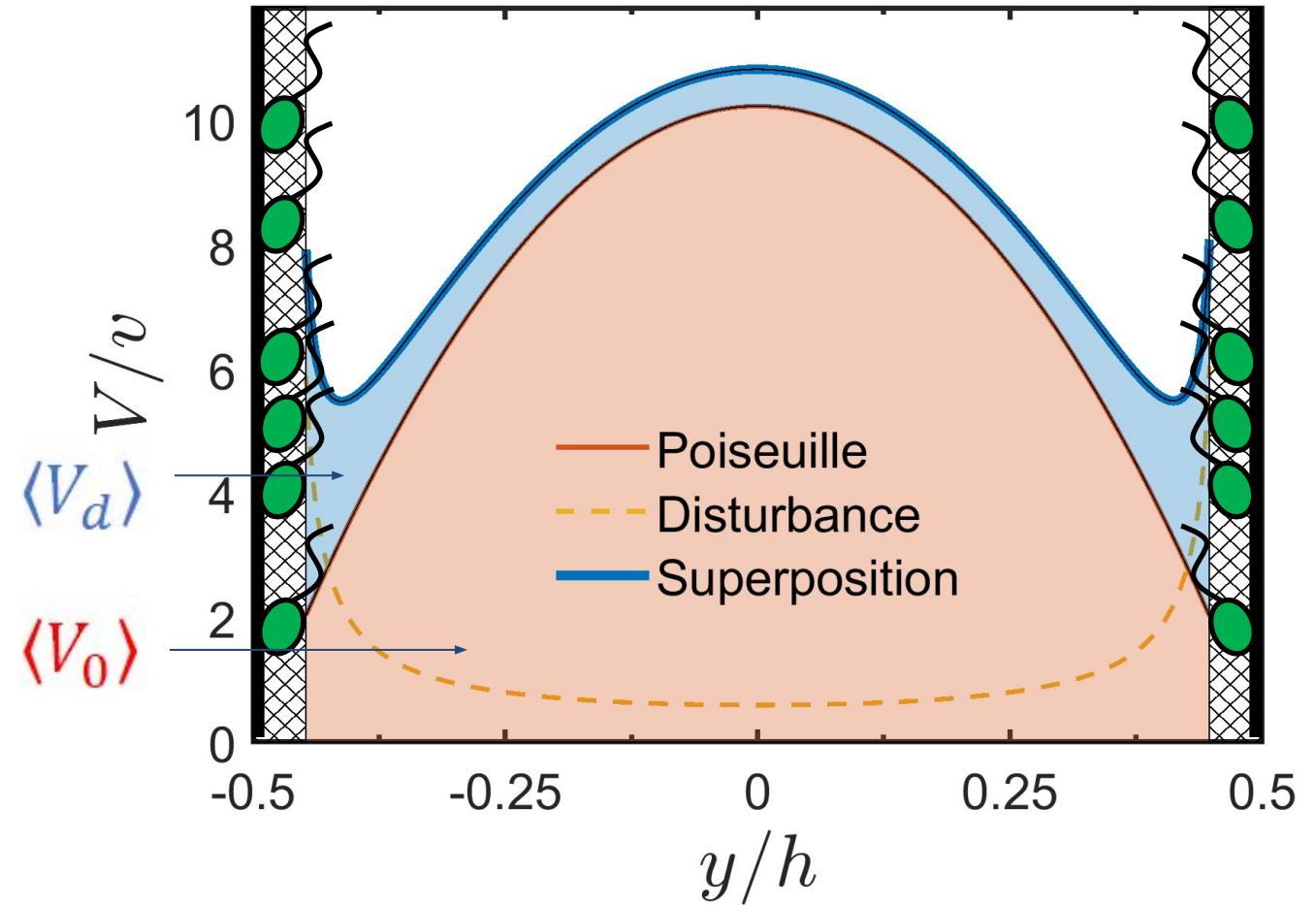
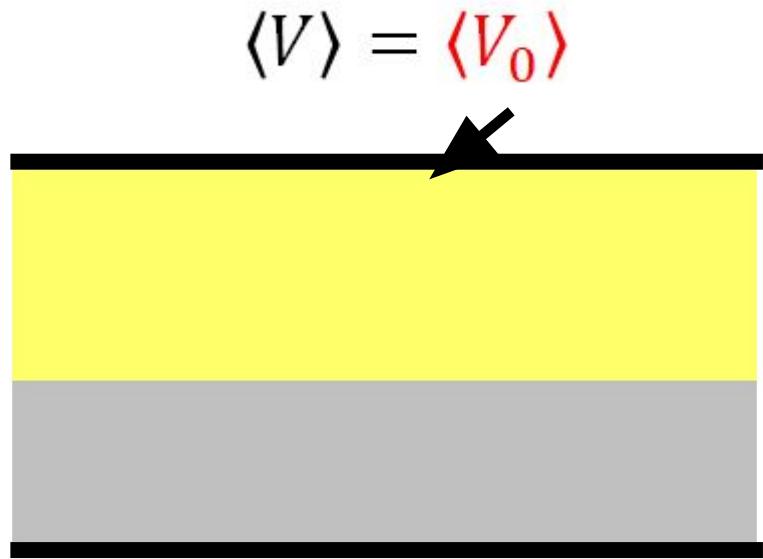
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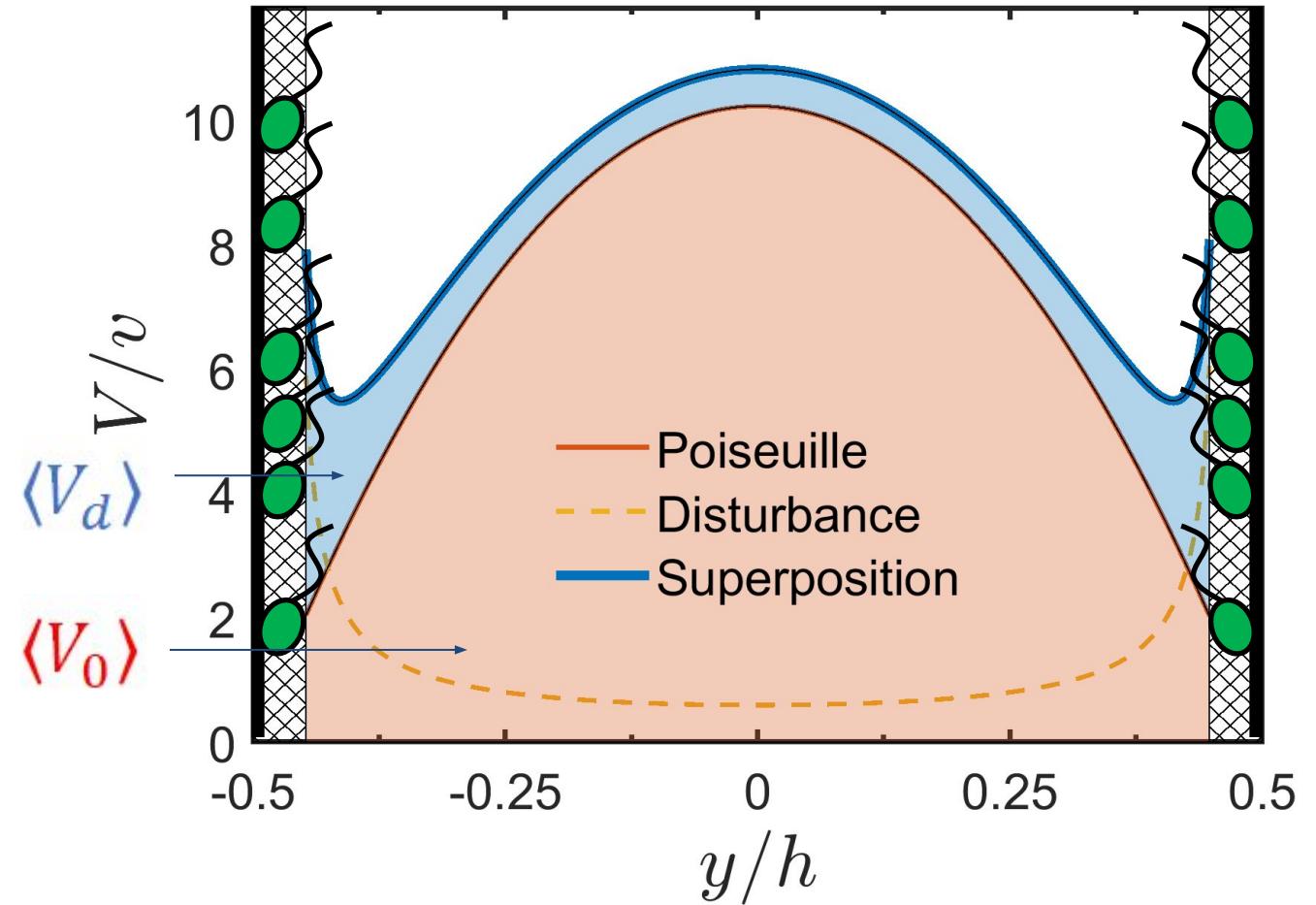
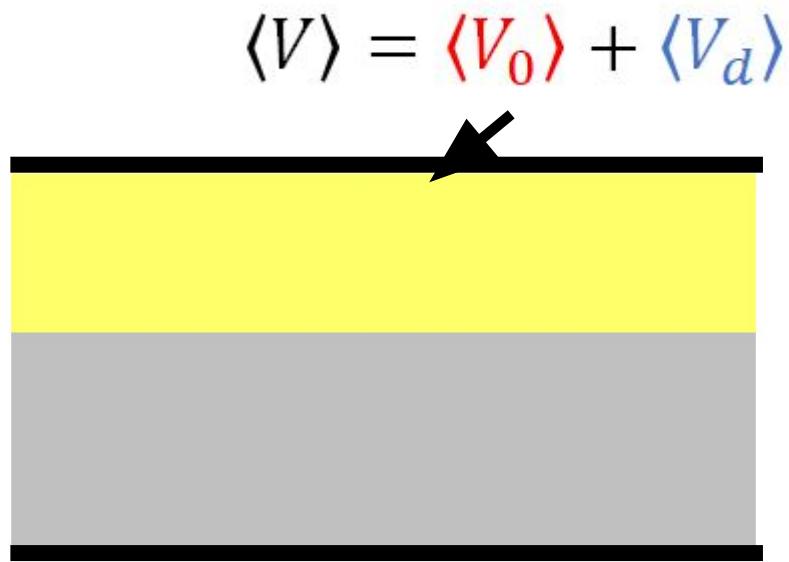
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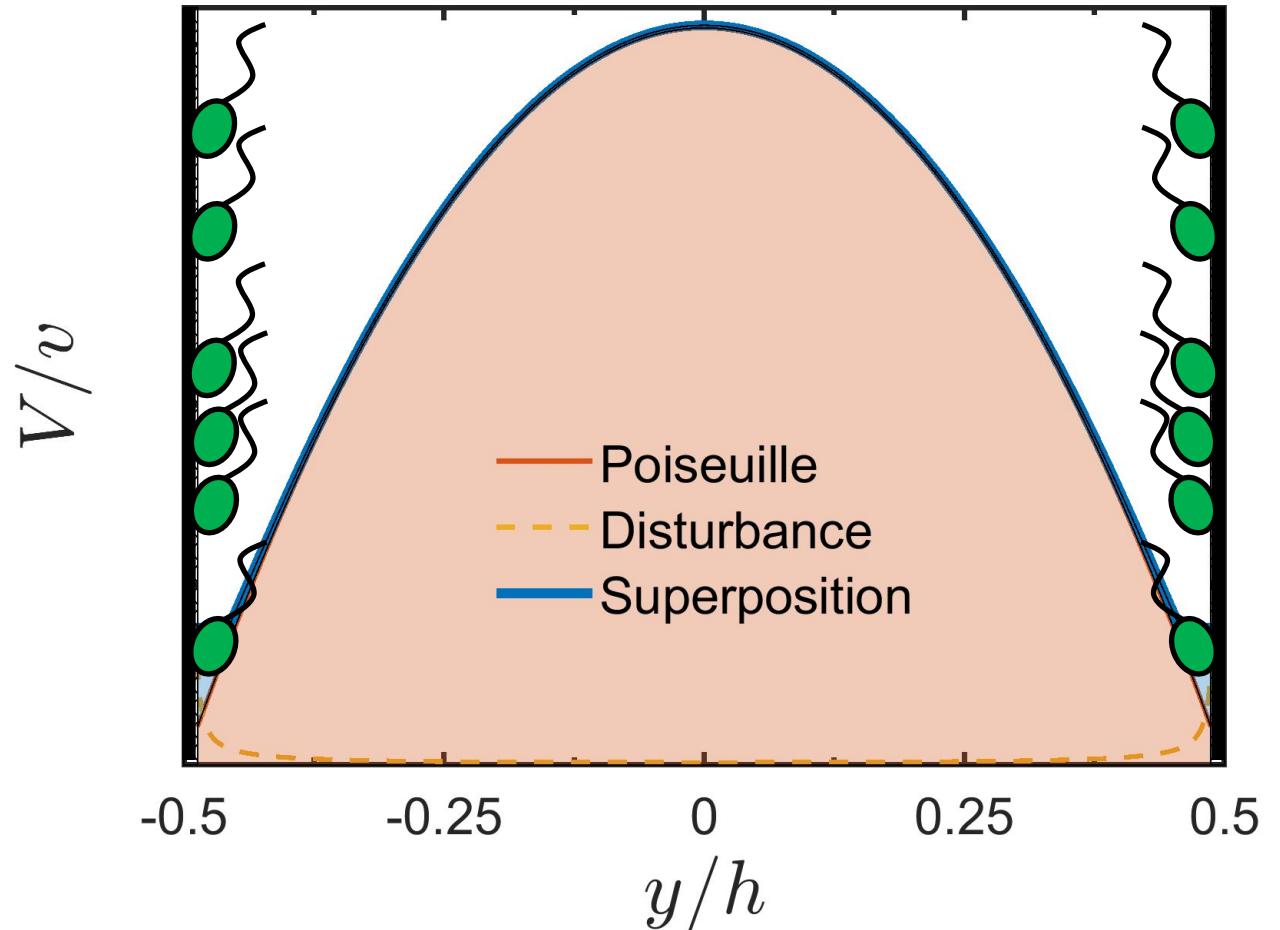
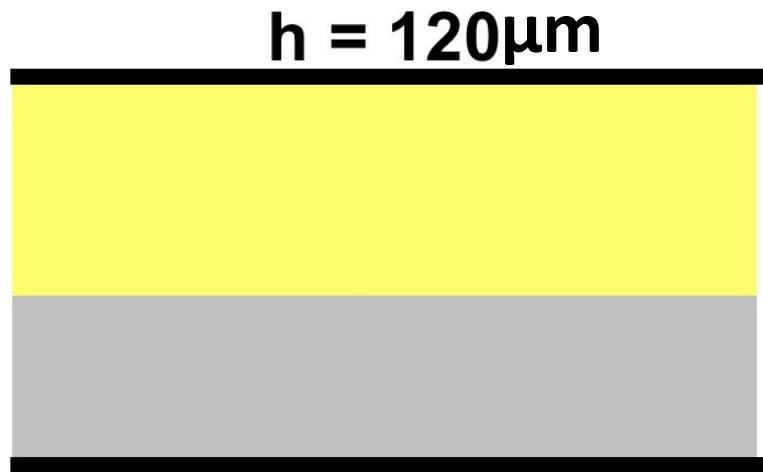
# Disturbance velocity leads to reduced viscosity



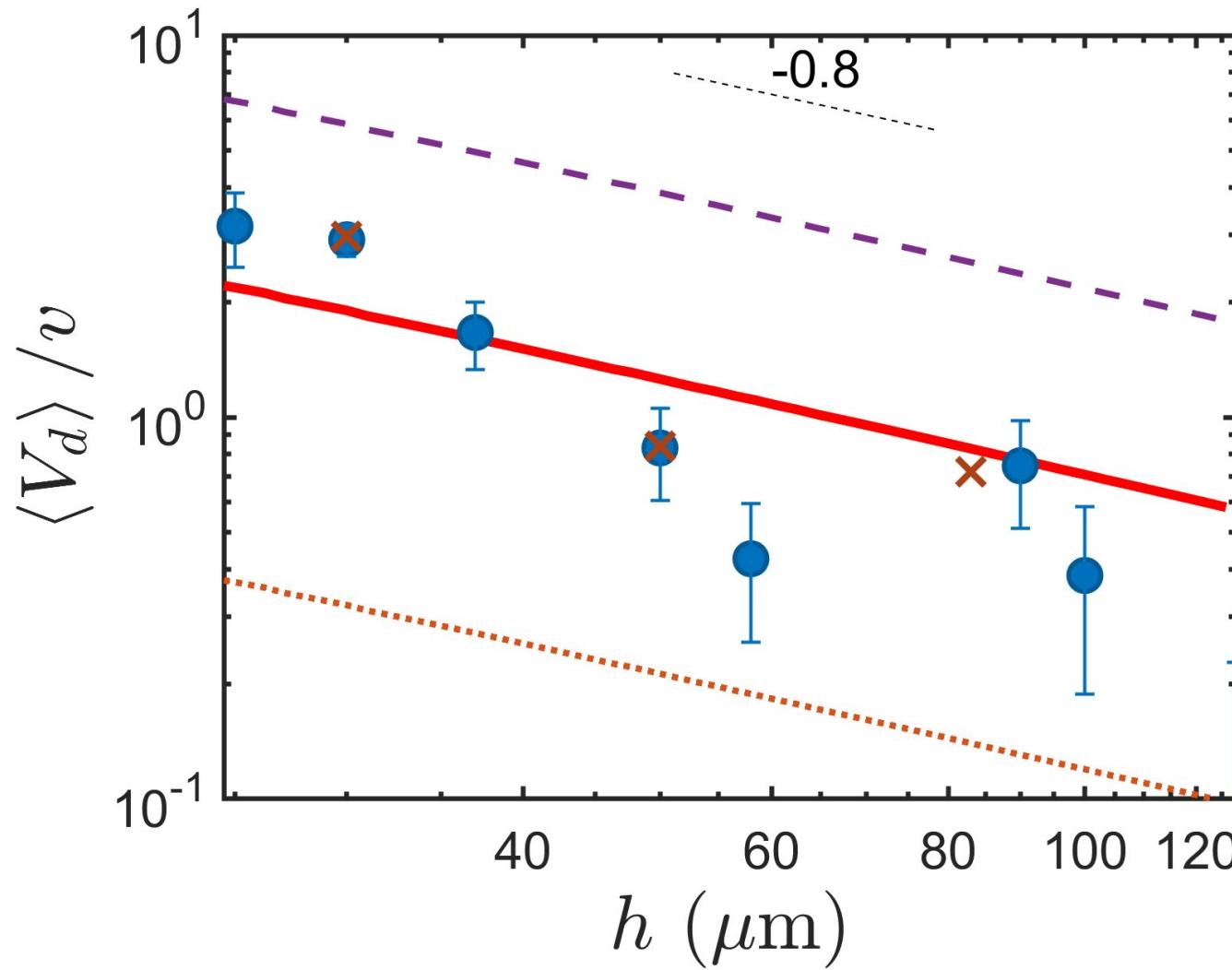
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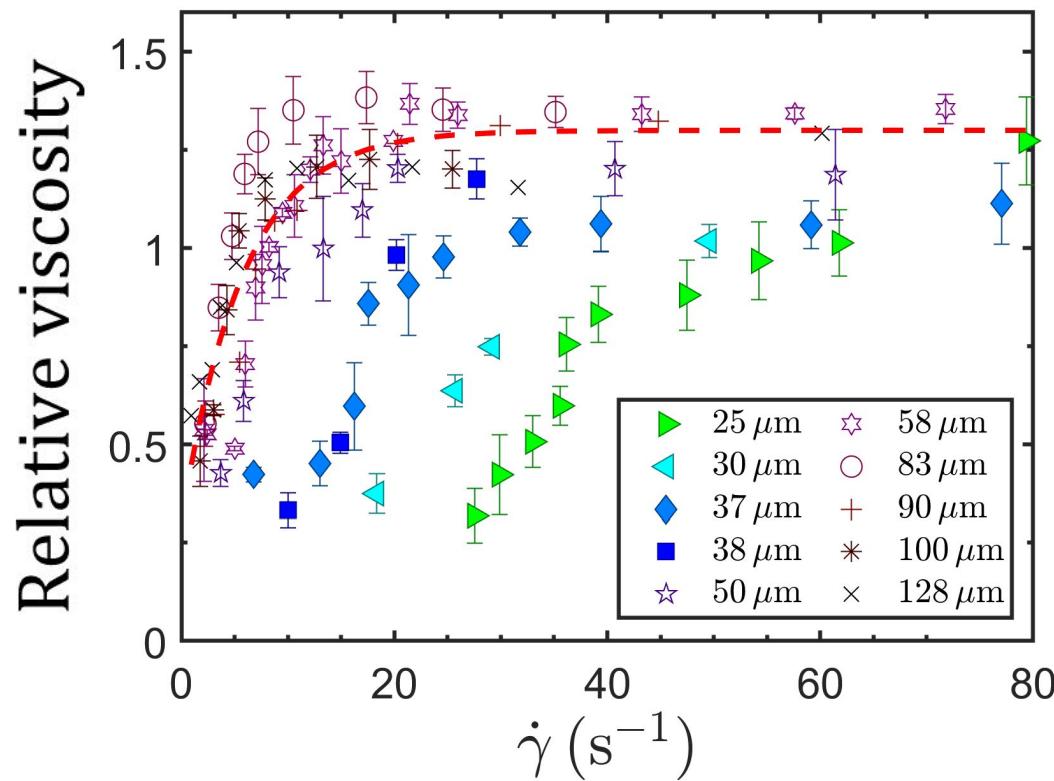


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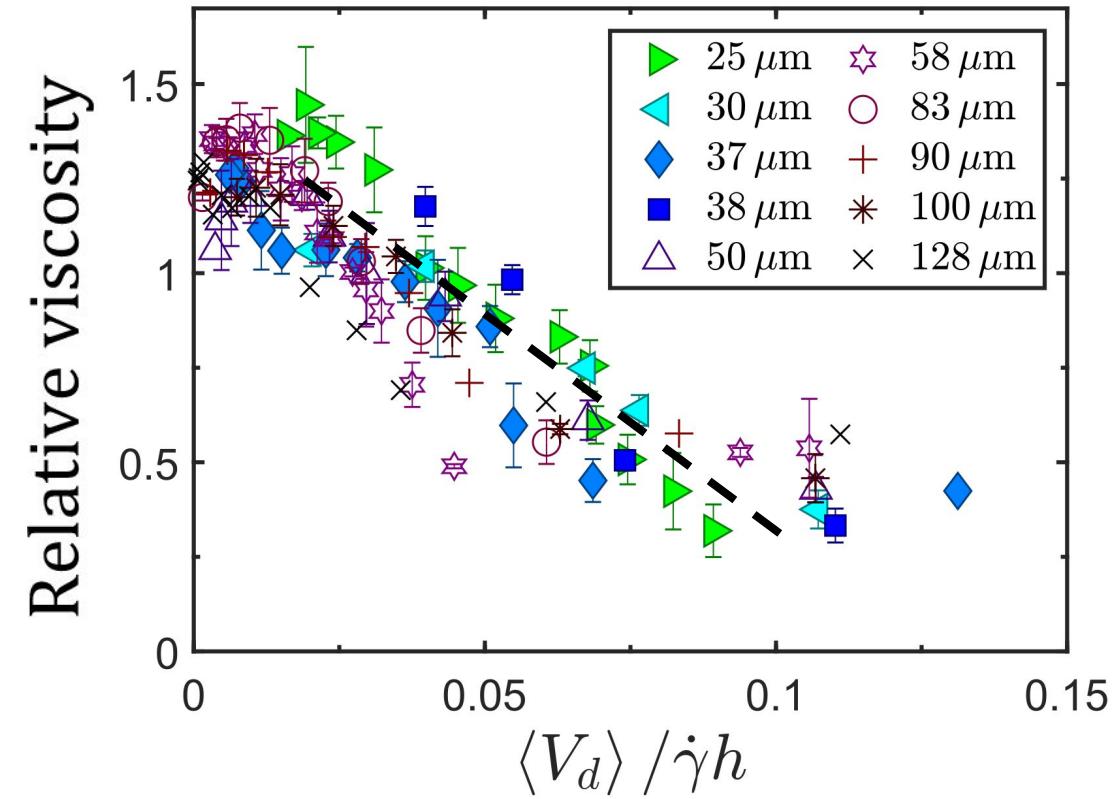
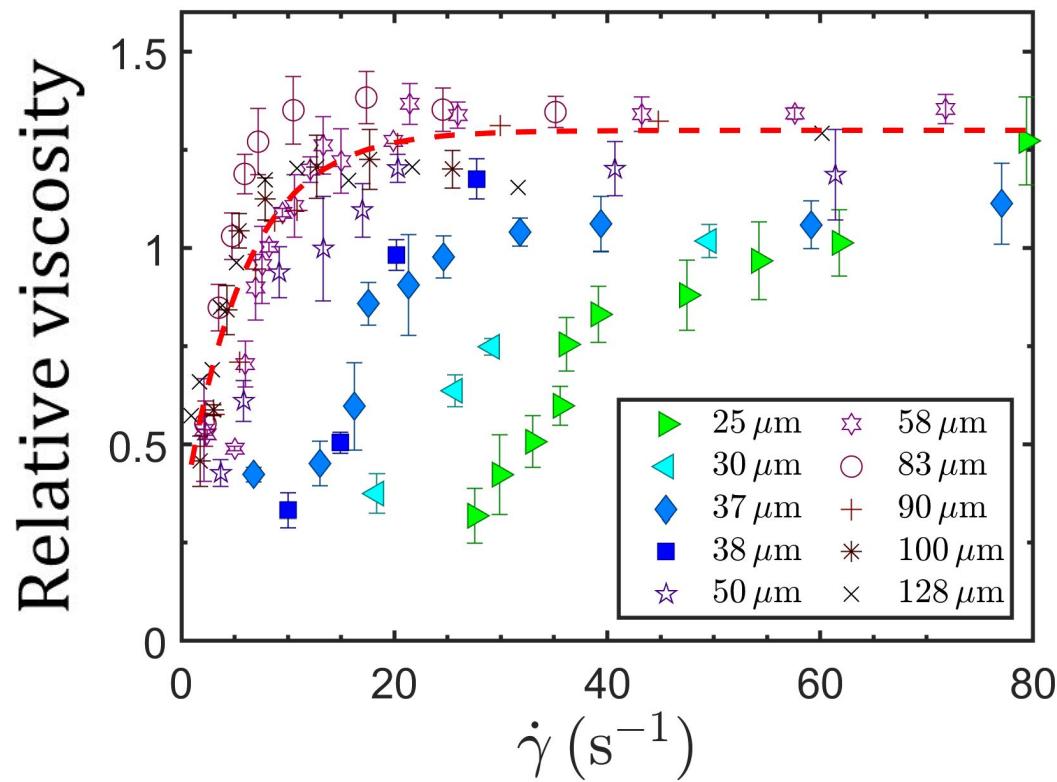
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$$\eta = \eta_b \left( 1 - \frac{6\langle V_d \rangle}{\dot{\gamma} h} \right)$$



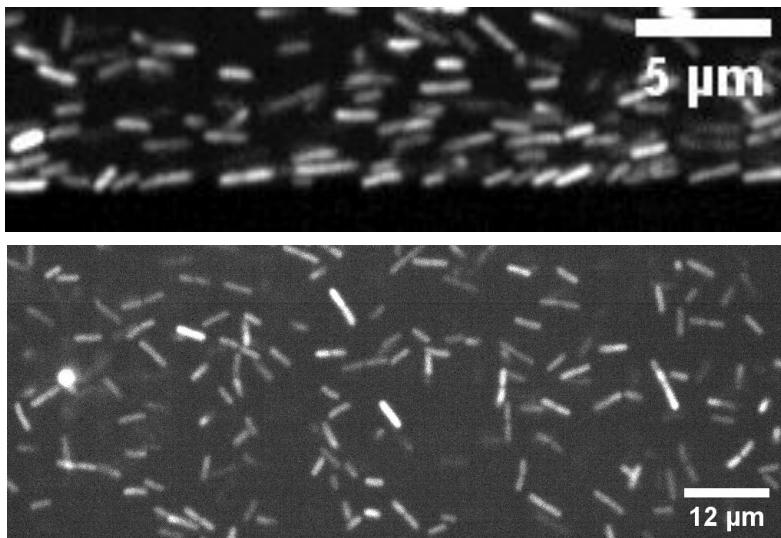
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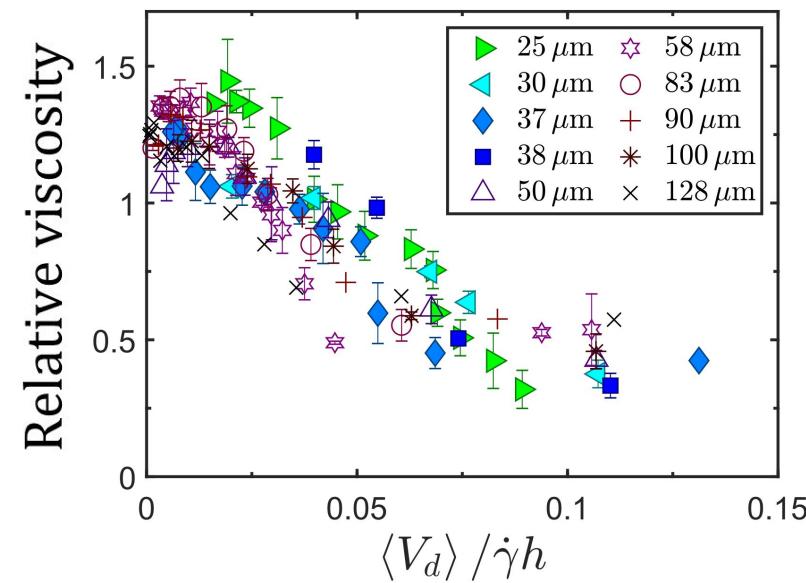
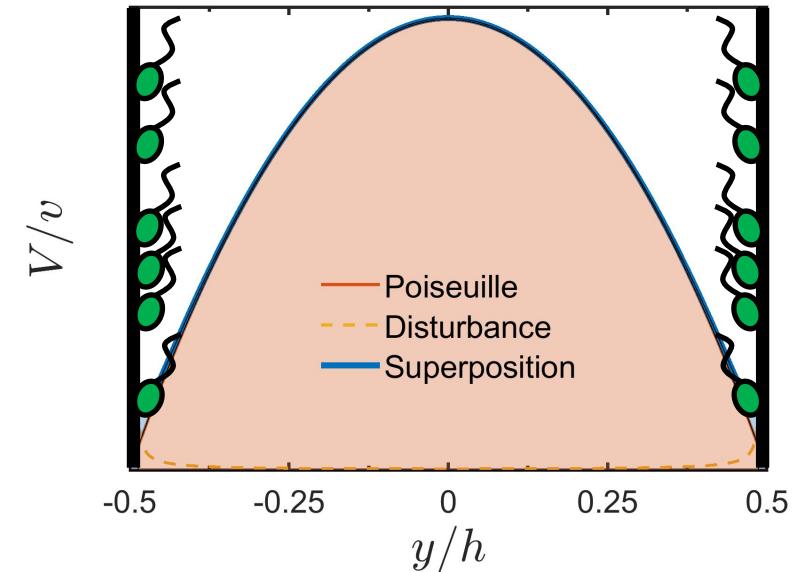


# Conclusions

- Confinement reduces the viscosity of *E. coli* suspensions
- A new mechanism of viscosity reduction due to upstream swimming boundary layer of *E. coli*



Liu, Z., Zhang, K. & Cheng, X., *Rheol Acta* (2019) **58**: 439



# Acknowledgment

## Group members

Dr. Yi Peng

Dr. Xiaolei Ma

Seunghwan Shin

Yangming Kou

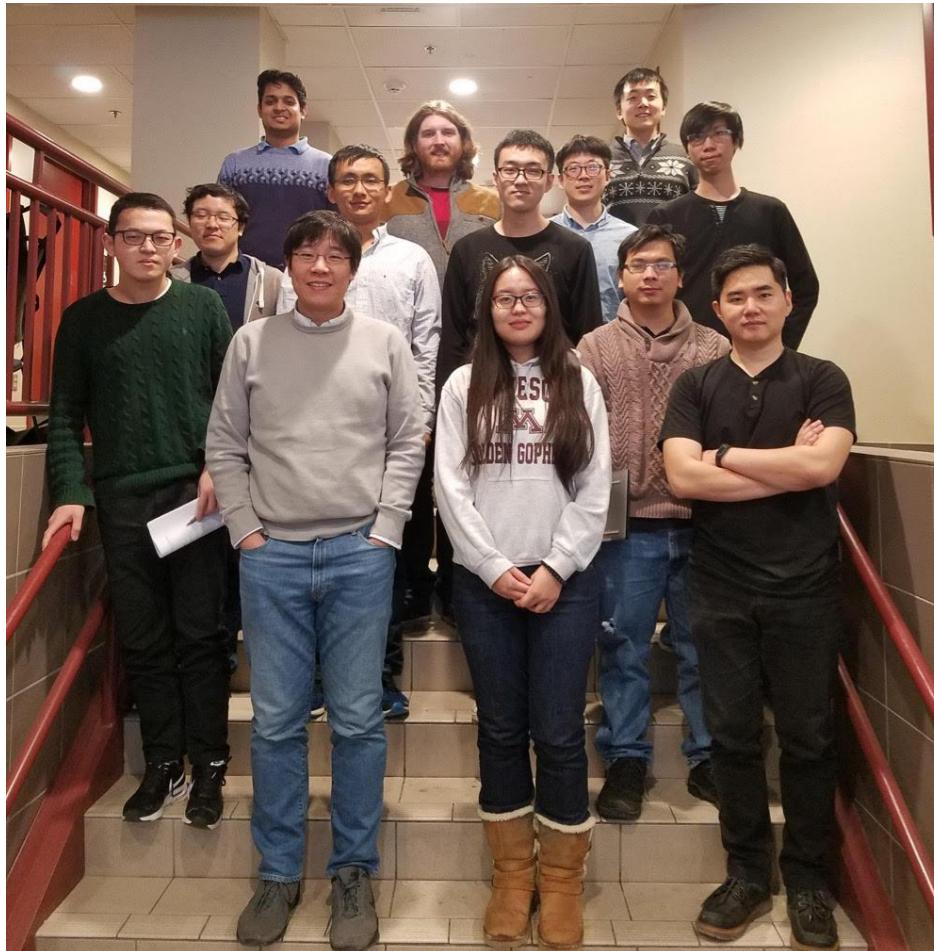
Ting-Pi Sun

Chen Fan

Shashank Kamdar

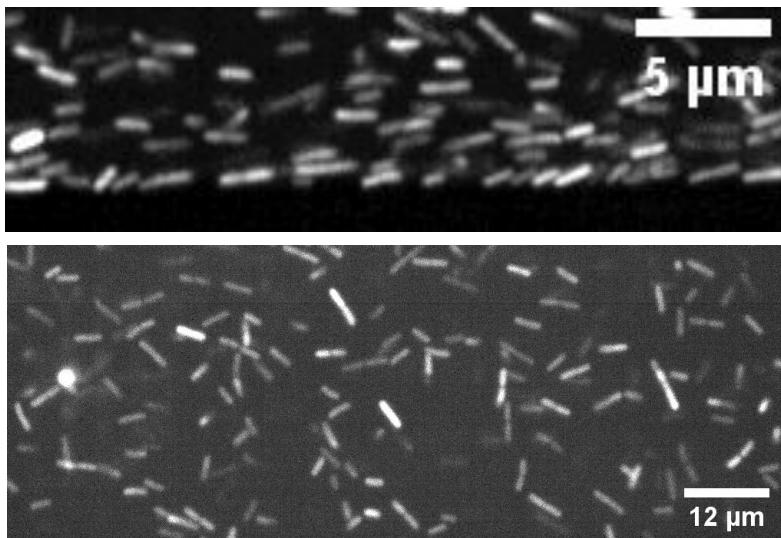
Dipanjan Ghosh

Yiming Qiao



# Conclusions

- Confinement reduces the viscosity of *E. coli* suspensions
- A new mechanism of viscosity reduction due to upstream swimming boundary layer of *E. coli*



Liu, Z., Zhang, K. & Cheng, X., *Rheol Acta* (2019) **58**: 439

